

Fundamentals of Earth's Atmospheric Structure & Circulation (with some comments on the Global Ocean)

AOSC 680

Ross Salawitch

Class Web Sites:

<http://www2.atmos.umd.edu/~rjs/class/fall2024>

<https://umd.instructure.com/courses/1367293>

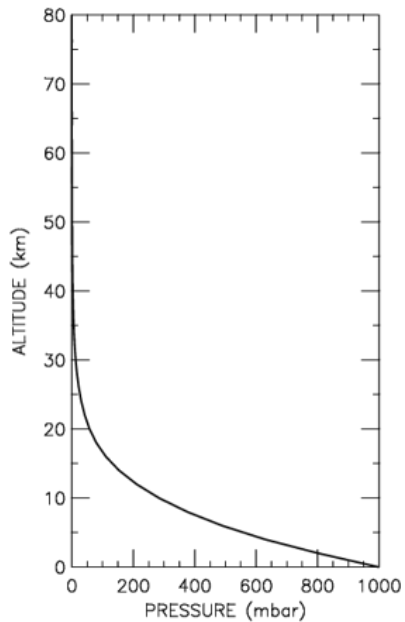
Goals:

- 1) Barometric law (pressure vs height)
- 2) Thermal structure (temperature vs height)
- 3) Geostrophy (balance of pressure force & Coriolis Force \Rightarrow storms)
- 4) Ferrel circulation (mean circulation Earth's atmosphere \Rightarrow climate regimes)
- 5) Features of the global ocean temperature and circulation

Lecture 3

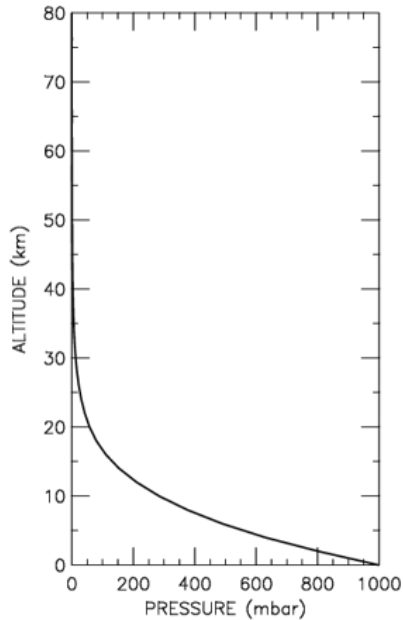
5 September 2024

Pressure versus Altitude



- **Pressure = Force per unit area**
- **Graph shows how “force” of atmosphere varies as a function of altitude**
- **Pressure shown in units of mbar : 1 mbar = 10^3 dynes/cm²**
- **1 dyne = gm cm / sec²; therefore 1 mbar = 10^3 gm / cm sec²**
- **Also:**
 - **European community prefers to write hPa; 1 hPa is exactly equal to 1 mbar**
 - **1 atmosphere = p/p_{STANDARD} , where $p_{\text{STANDARD}} = 1013.25$ mbar (or 1013.25 hPa)**

Pressure versus Altitude



Derivation of the Barometric Law involves use of the Ideal Gas Law:

$$p \text{ Vol} = n R T$$

where p is pressure, Vol is volume, n is the number of moles of a gas,

R is the gas constant ($8.3143 \times 10^7 \frac{\text{ergs}}{\text{K mole}}$), and T is temperature

as shown on Extra Slide 1 at end of Class Notes (you will not be tested on this!)

- Barometric law describes the variation of Earth's pressure with respect to altitude:

$$\text{Pressure (z)} = \text{Pressure (surface)} \times e^{-z/H}$$

where H is called the “scale height”

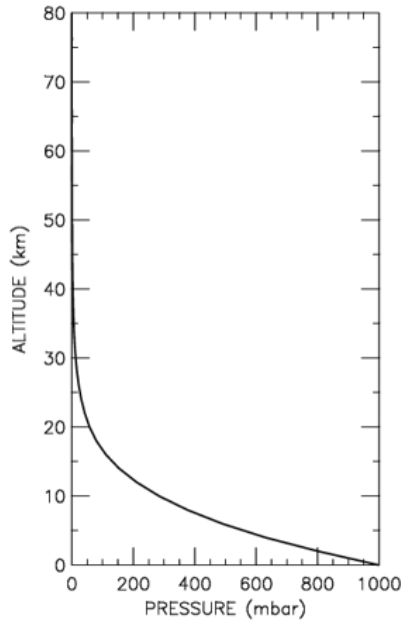
$$\text{Can show } H = R_{\text{EARTH}} T(z) / \text{grav} ,$$

$$\text{Since } R_{\text{EARTH}} = 2.88 \times 10^6 \text{ ergs / K gm}$$

$$\text{grav} = 981 \text{ cm sec}^{-2} \quad \text{and} \quad T(\text{lower trop}) \approx 272 \text{ K}$$

$$\text{then } H(z=0) = 8.0 \times 10^5 \text{ cm} = 8 \text{ km}$$

Pressure versus Altitude



In modern atmospheric sciences, the most handy version of the Ideal Gas Law is:

$$p = M k T$$

where p is pressure (force per unit area), M is number density (molecules/volume), k is Boltzmann's constant (1.38×10^{-16} ergs/K), and T is temperature.

If p is given in units of mbar (or hPa), M is in units of $\frac{\text{molecules}}{\text{cm}^3}$, and T is in K, then can show k must be $1.38 \times 10^{-19} \frac{\text{mbar cm}^3}{\text{K molecules}}$

- **Barometric law describes the variation of Earth's pressure with respect to altitude:**

$$\text{Pressure (z)} = \text{Pressure (surface)} \times e^{-z/H}$$

where H is called the “scale height”

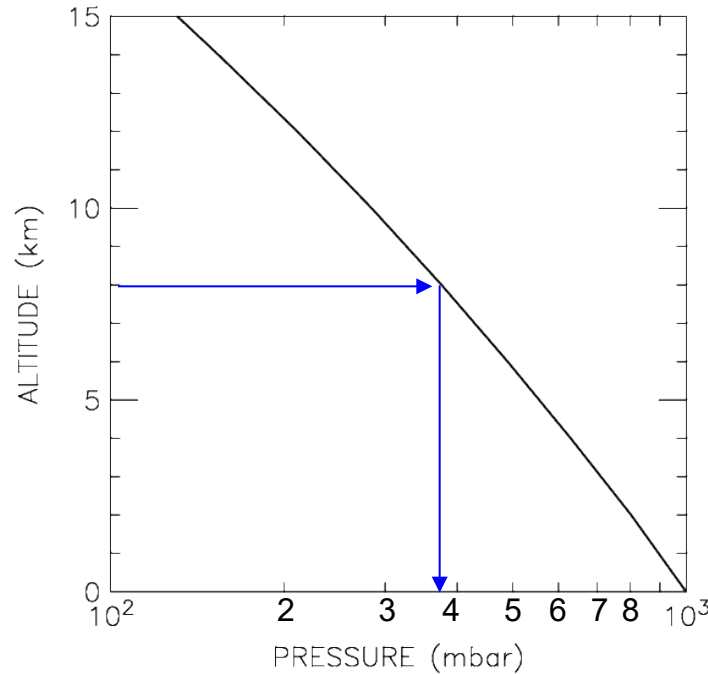
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Pressure versus Altitude



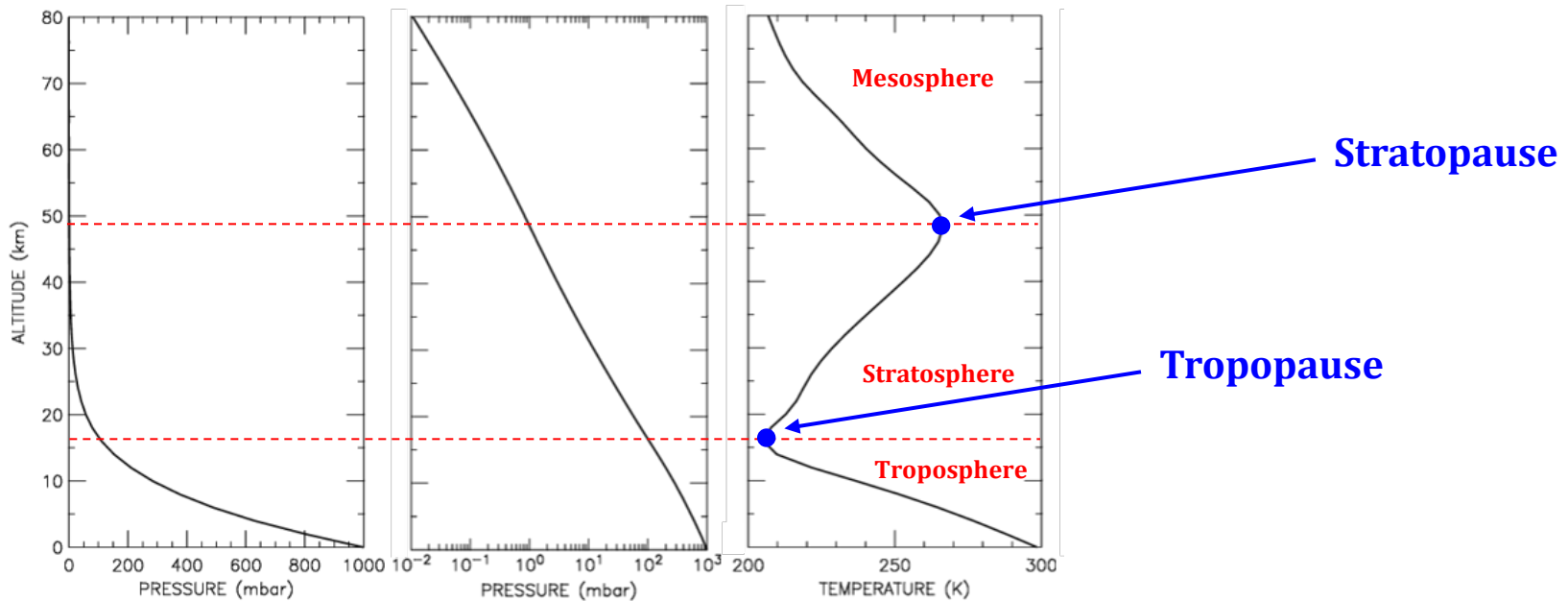
$$p(z=0) = 1013.25 \text{ mbar}$$
$$p(z=8 \text{ km}) =$$

- Barometric law describes the variation of Earth's pressure with respect to altitude:

$$\text{Pressure}(z) = \text{Pressure}(\text{surface}) \times e^{-z/H}$$

Let's take a closer look at log pressure versus altitude, in the troposphere

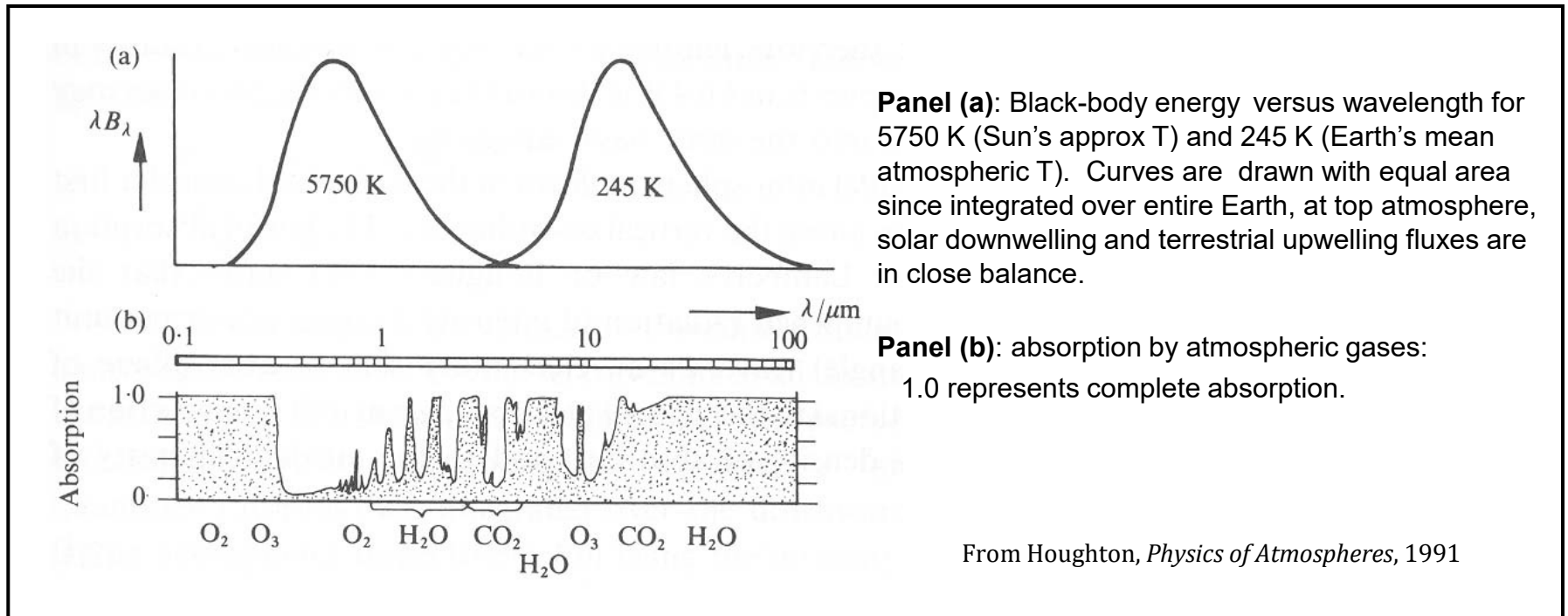
Temperature versus Altitude



- T falls wrt increasing altit until the tropopause, then rises wrt altit until the stratopause, then falls wrt to rising altitude

Atmospheric Radiation

- Solar irradiance (downwelling) at top of atmosphere occurs at wavelengths between ~ 200 and 2000 nm (~ 5750 K “black body” temperature)
- Thermal irradiance (upwelling) at top of the atmosphere occurs at wavelengths between ~ 5 and 50 μm (~ 245 K “black body” temperature)



Atmospheric Radiation

THE GREENHOUSE EFFECT

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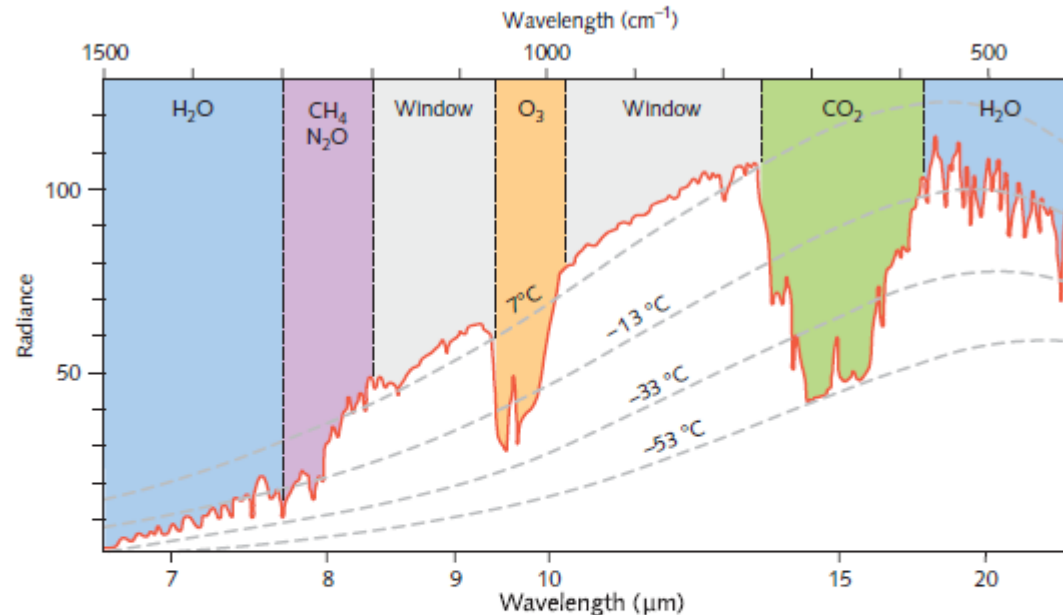
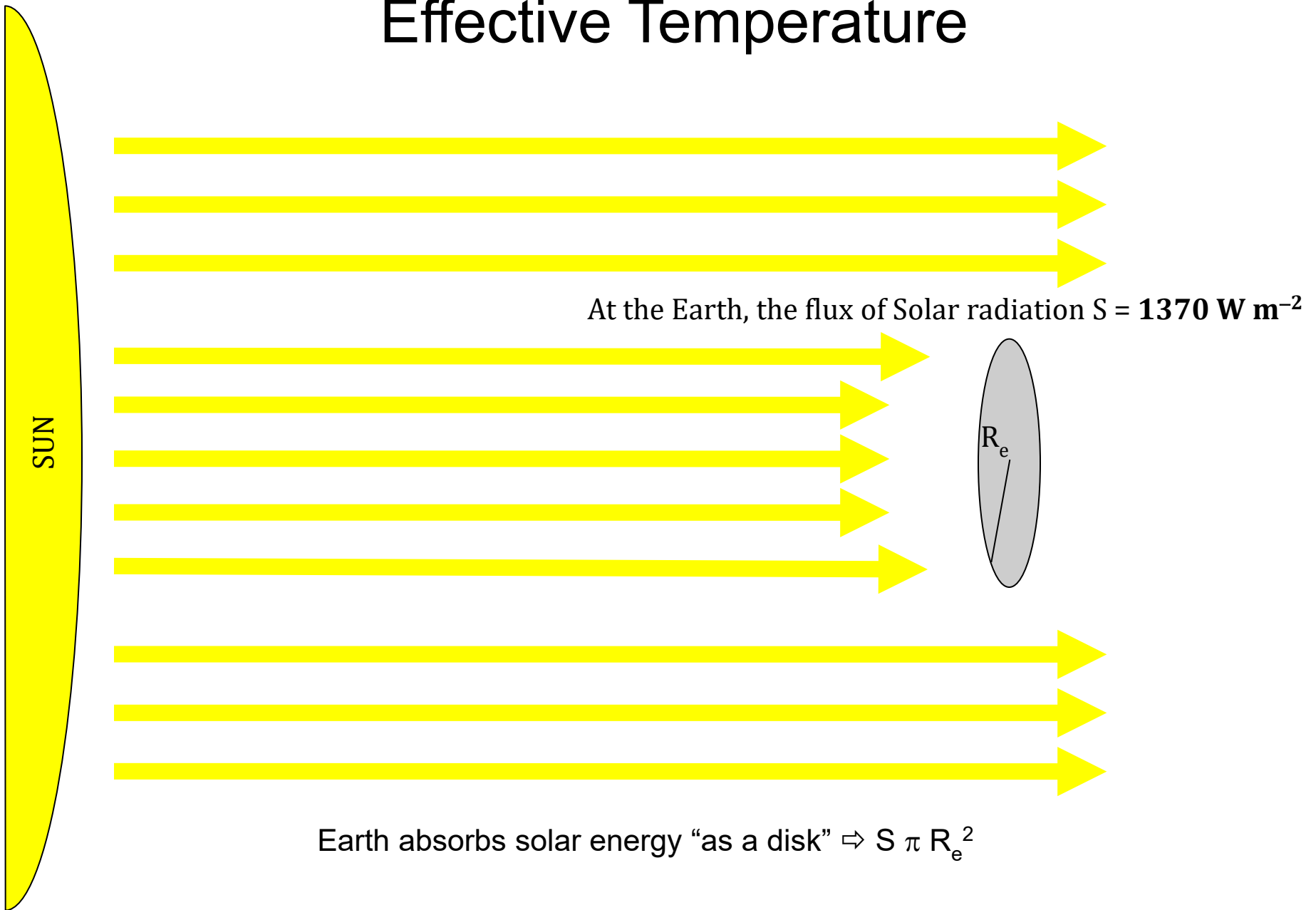


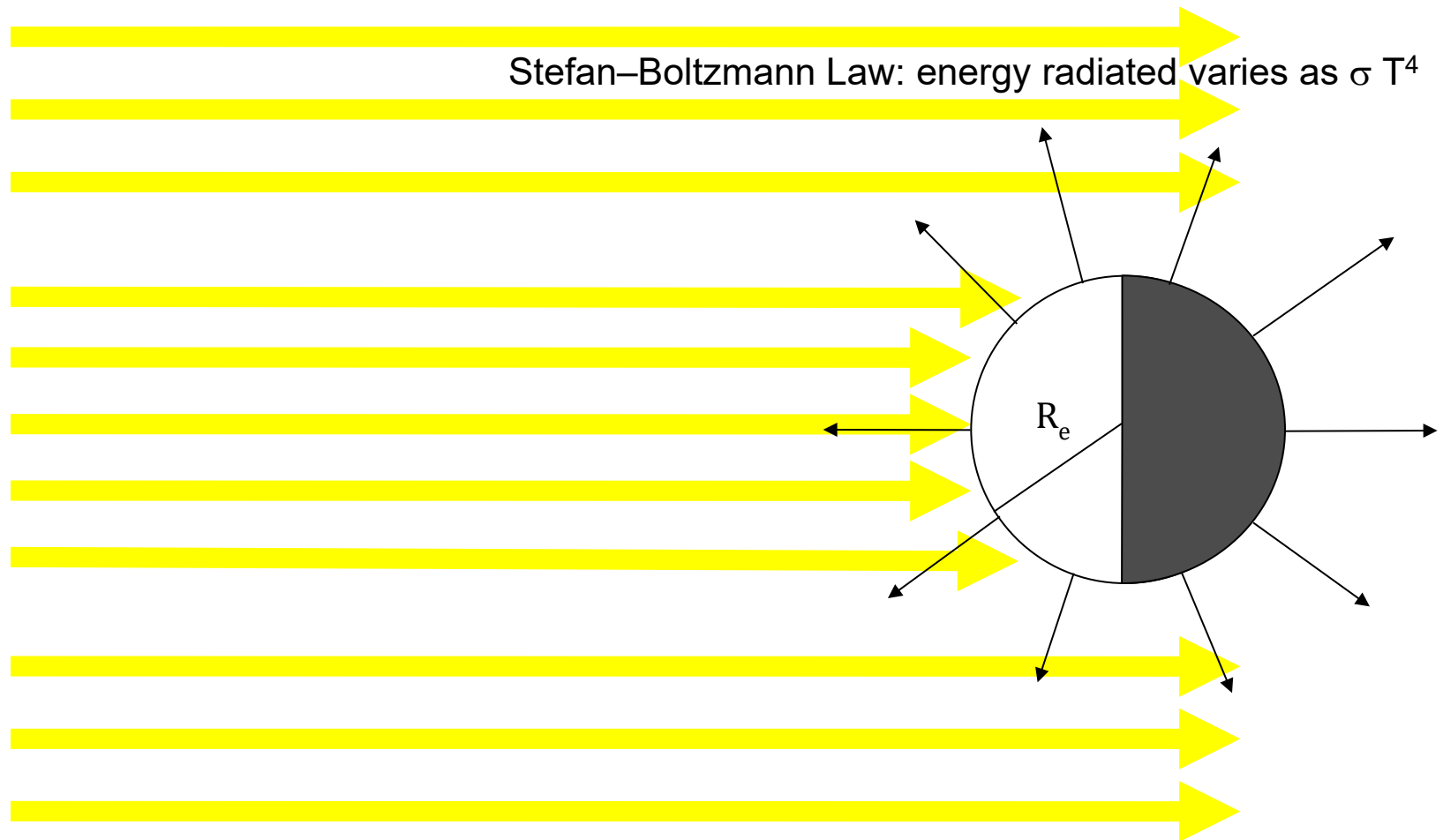
Figure 2.5 Thermal radiation in the infrared region (the visible part of the spectrum is between about 0.4 and 0.7 μm) emitted from the Earth's surface and atmosphere as observed over the Mediterranean Sea from a satellite instrument orbiting above the atmosphere, showing parts of the spectrum where different gases contribute to the radiation. Between the wavelengths of about 8 and 14 μm , apart from the ozone band, the atmosphere, in the absence of clouds, is substantially transparent; this is part of the spectrum called a 'window' region. Superimposed on the spectrum are curves of radiation from a black body at 7°C, -13°C, -33°C and -53°C. The units of radiance are milliwatts per square metre per steradian per wavenumber.

Fig 2.5, *Global Warming (5th Edition)*, Houghton

Effective Temperature



Effective Temperature



Earth emits thermal energy "as a sphere" $\Rightarrow \sigma 4\pi R_e^2 T_{\text{EFF}}^4$

Effective Temperature

Earth absorbs solar energy “as a disk” $\Rightarrow (1 - \text{Albedo}) \times S \pi R_e^2$

Earth emits thermal energy “as a sphere” $\Rightarrow \sigma 4\pi R_e^2 T_{\text{EFF}}^4$

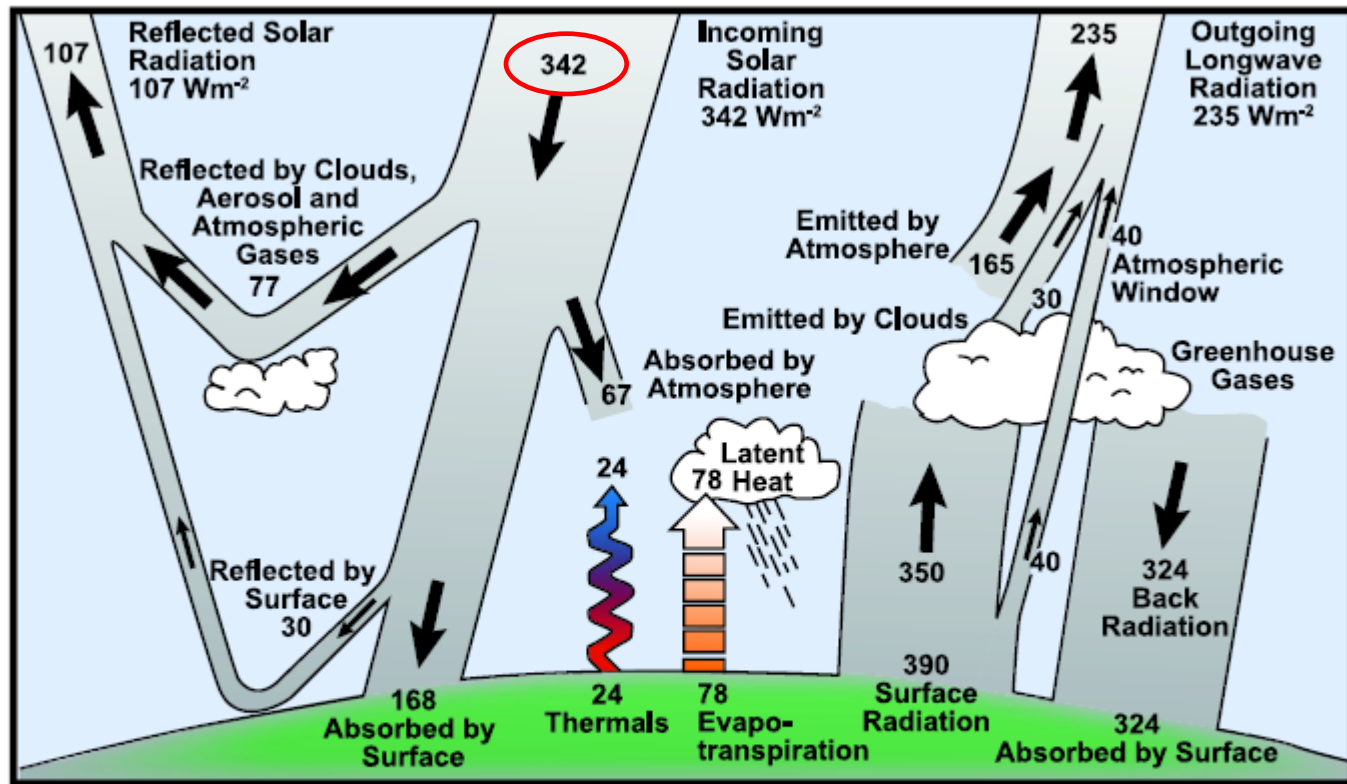
$$(1 - \text{Albedo}) \times S = 4 \sigma T_{\text{EFF}}^4$$

or

$$T_{\text{EFF}} = \{ (1 - \text{Albedo}) \times S / 4 \sigma \}^{1/4}$$

Effective Temperature

Let's take a closer look at $S = 1370 \text{ W m}^{-2}$



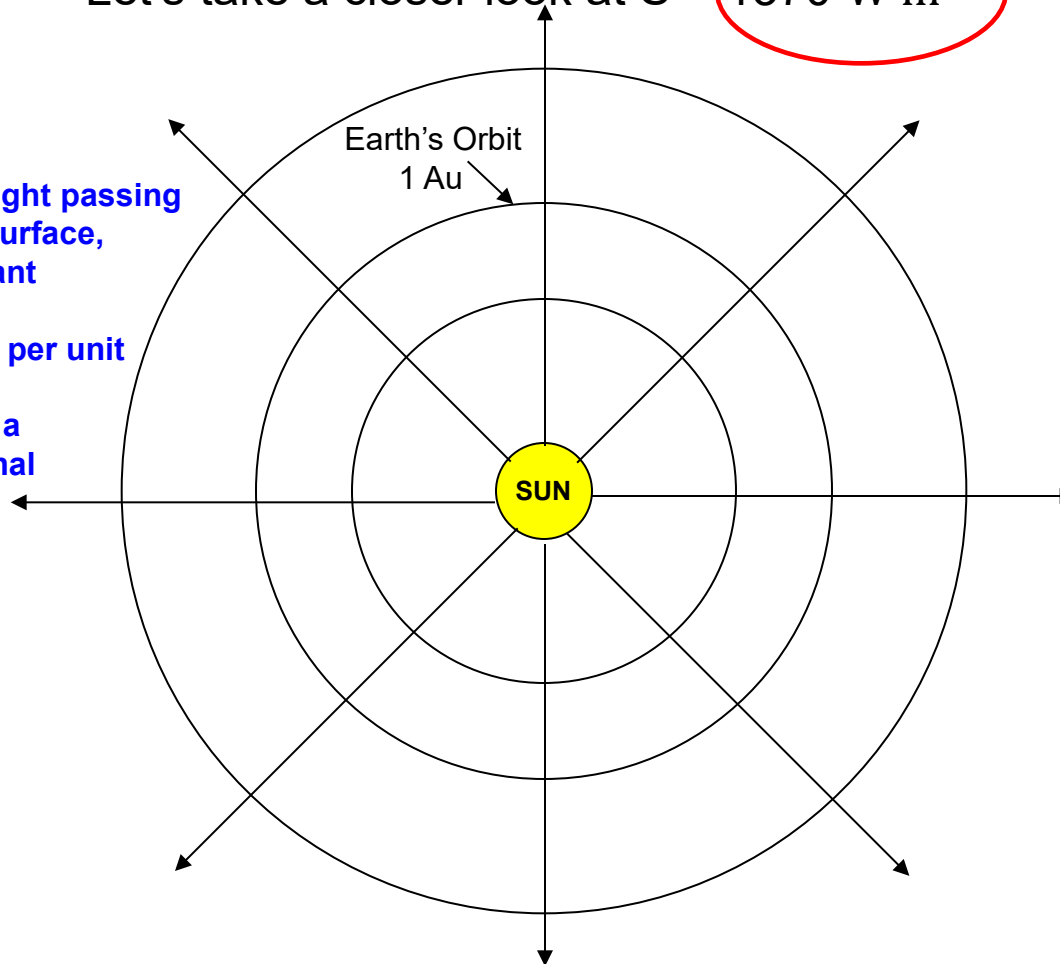
FAQ 1.1, Figure 1. Estimate of the Earth's annual and global mean energy balance. Over the long term, the amount of incoming solar radiation absorbed by the Earth and atmosphere is balanced by the Earth and atmosphere releasing the same amount of outgoing longwave radiation. About half of the incoming solar radiation is absorbed by the Earth's surface. This energy is transferred to the atmosphere by warming the air in contact with the surface (thermals), by evapotranspiration and by longwave radiation that is absorbed by clouds and greenhouse gases. The atmosphere in turn radiates longwave energy back to Earth as well as out to space. Source: Kiehl and Trenberth (1997).

Effective Temperature

Let's take a closer look at $S = 1370 \text{ W m}^{-2}$

The total amount of sunlight passing through each spherical surface, of various radii, is constant

Therefore the energy (W) per unit area (m^{-2}) decreases wrt distance from the Sun in a manner that is proportional to: _____



- Notes: 1) Au, or Astronomical Unit, is a measure of the distance of a planet from the Sun, normalized by the mean distance of Earth from the Sun. So by definition, **Earth's orbit is 1 Au from the Sun**
- 2) The diagram above represents orbits as perfect spheres, which is suitable for our study of effective temperatures. In reality, of course, planets orbit the Sun in an elliptical manner.

$$T_{\text{EFF}} = \{ (1 - \text{Albedo}) \times S / 4 \sigma \}^{1/4}$$

Those with “Earth”: find T_{EFF} for Earth, using:

$$\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$$

$$S = 1370 \text{ W m}^{-2}$$

$$\text{Albedo} = 0.3$$

Those with “Mars”: find T_{EFF} for **Mars** using:

$$\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$$

$$S = 1370 \text{ W m}^{-2}$$

$$\text{Albedo} = 0.17$$

Distance from Sun = 1.5 AU

Those with “Venus”: find T_{EFF} for **Venus** using:

$$\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$$

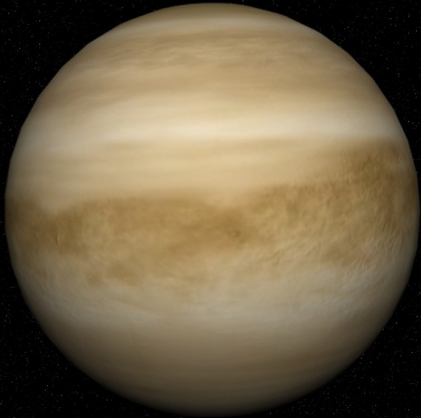
$$S = 1370 \text{ W m}^{-2}$$

$$\text{Albedo} = 0.75$$

Distance from Sun = 0.72 AU

Effective Temperature

My Favorite Planets



Venus:

$$T_{\text{SURFACE}} \approx 753 \text{ K}$$

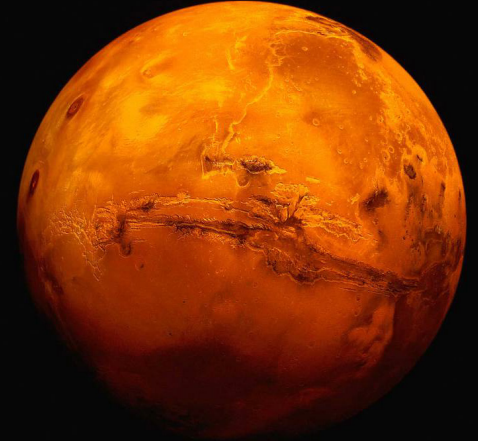
$$T_{\text{EFFECTIVE}} \approx ???$$



Earth:

$$T_{\text{SURFACE}} \approx 288 \text{ K}$$

$$T_{\text{EFFECTIVE}} \approx ???$$



Mars

$$T_{\text{SURFACE}} \approx 217 \text{ K}$$

$$T_{\text{EFFECTIVE}} \approx ???$$

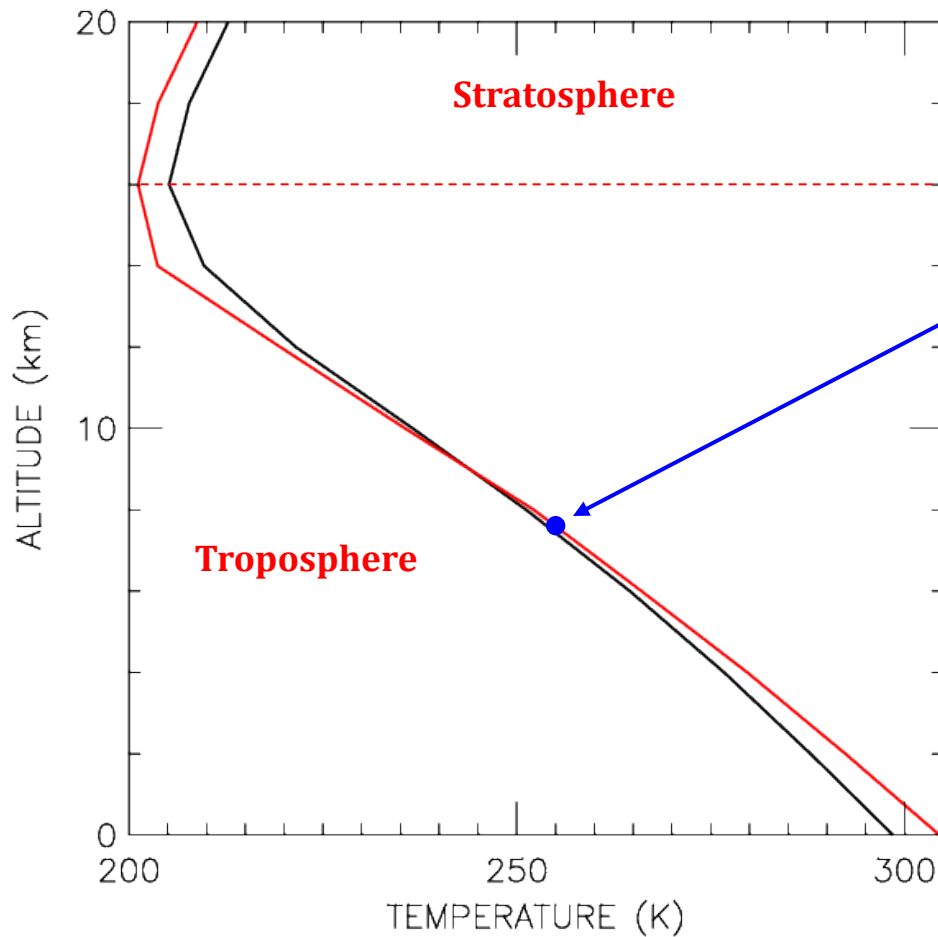
Geological Evolution of Earth's Atmosphere:

Earth, Mars, and Venus

	Earth	Venus	Mars
Radius (km)	6400	6100	3400
Mass (10^{24} kg)	6.0	4.9	0.6
Albedo	0.3	0.8	0.22
Distance from Sun (A.U.)	1	0.72	1.52
Surface Pressure (atm)	1	91	0.007
Surface Temperature (K)	$\sim 15^\circ\text{C}$	$\sim 460^\circ\text{C}$	-140°C to 20°C
N ₂ (mol/mol)	0.78	3.4×10^{-2}	2.7×10^{-2}
O ₂ (mol/mol)	0.21	6.9×10^{-5}	1.3×10^{-3}
CO ₂ (mol/mol)	3.7×10^{-4}	0.96	0.95
H ₂ O (mol/mol)	1×10^{-2}	3×10^{-3}	3×10^{-4}
SO ₂ (mol/mol)	1×10^{-9}	1.5×10^{-4}	Nil
Cloud Composition	H ₂ O	H ₂ SO ₄	Mineral Dust

Temperature versus Altitude

Let's take a closer look at $T_{\text{EFF}} = 255 \text{ K}$



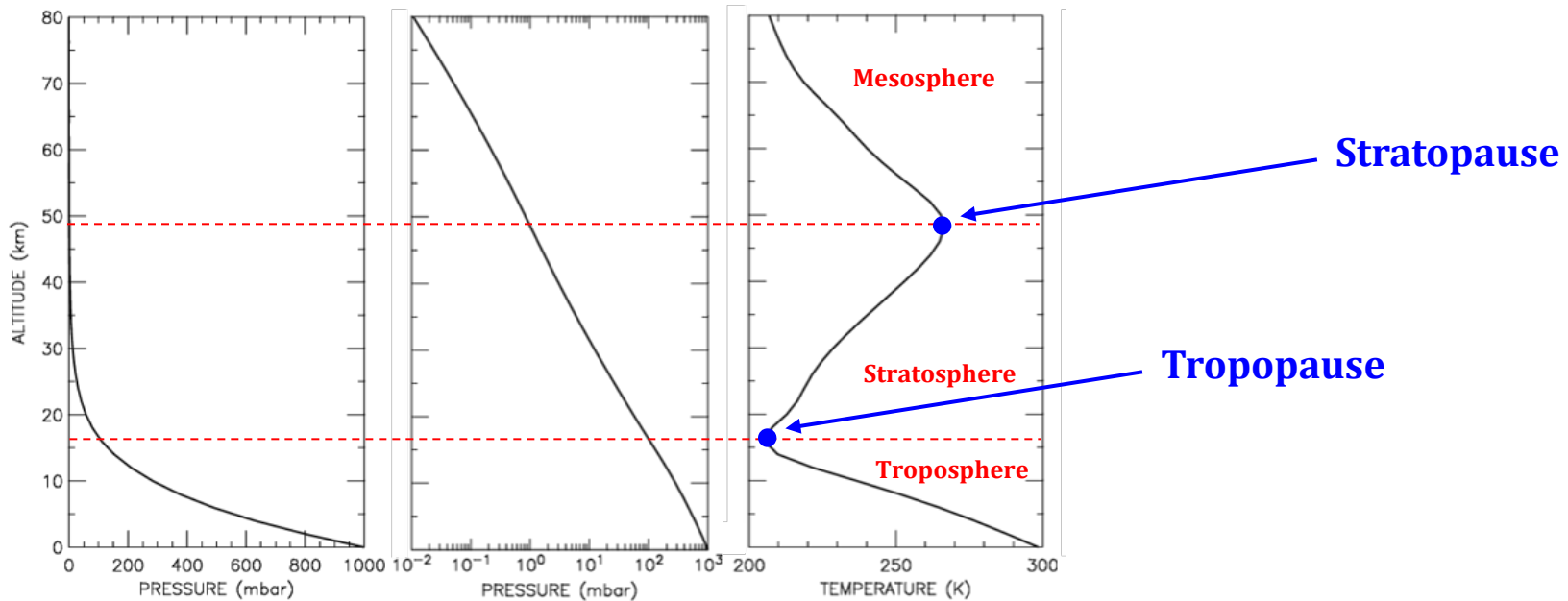
Altitude in troposphere where
 $T = 255 \text{ K}$

Termed Earth's mean radiating
altitude to space

As Earth warms in response
to rising GHGs, the lower troposphere
will warm, the stratosphere will cool,
and the mean radiating level
will likely rise slightly higher in altitude

Regardless, the temperature of the mean
radiating altitude will not change unless

Temperature versus Altitude



- T falls wrt increasing altit until the tropopause, then rises wrt altit until the stratopause, then falls wrt to rising altitude

If the troposphere is dry, $dT/dz = - \text{grav} / c_p$

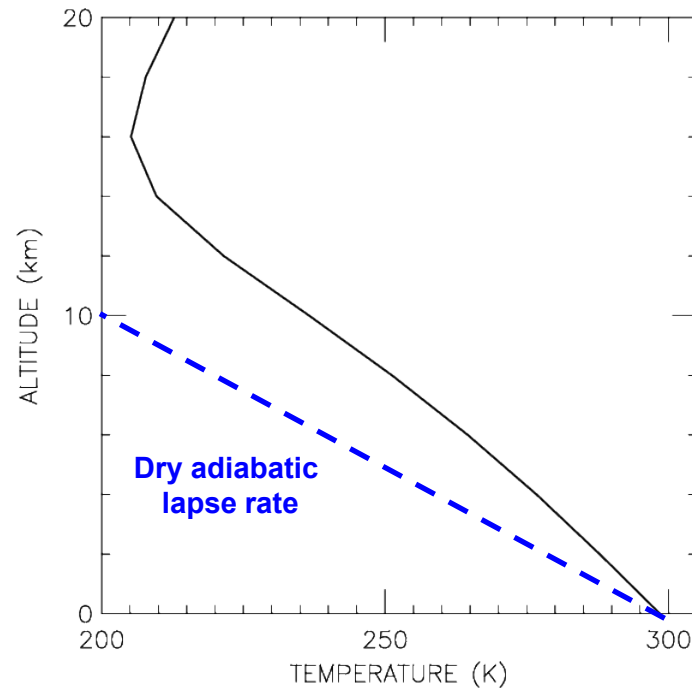
where c_p is specific heat of air at constant pressure = $1 \times 10^7 \text{ erg gm}^{-1} \text{ K}^{-1}$

Note: $1 \text{ erg} = 1 \text{ dyne cm} = \text{gm cm}^2 \text{ sec}^{-2}$

$$\Rightarrow dT/dz^{\text{DRY}} = - 981 \text{ cm sec}^{-2} / (10^7 \text{ cm}^2 \text{ sec}^{-2} \text{ K}^{-1}) \times 10^5 \text{ cm/km} = 9.8 \text{ K / km}$$

Dry adiabatic lapse rate

Temperature versus Altitude



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If the troposphere is dry, $dT/dz = - \text{grav} / c_p$

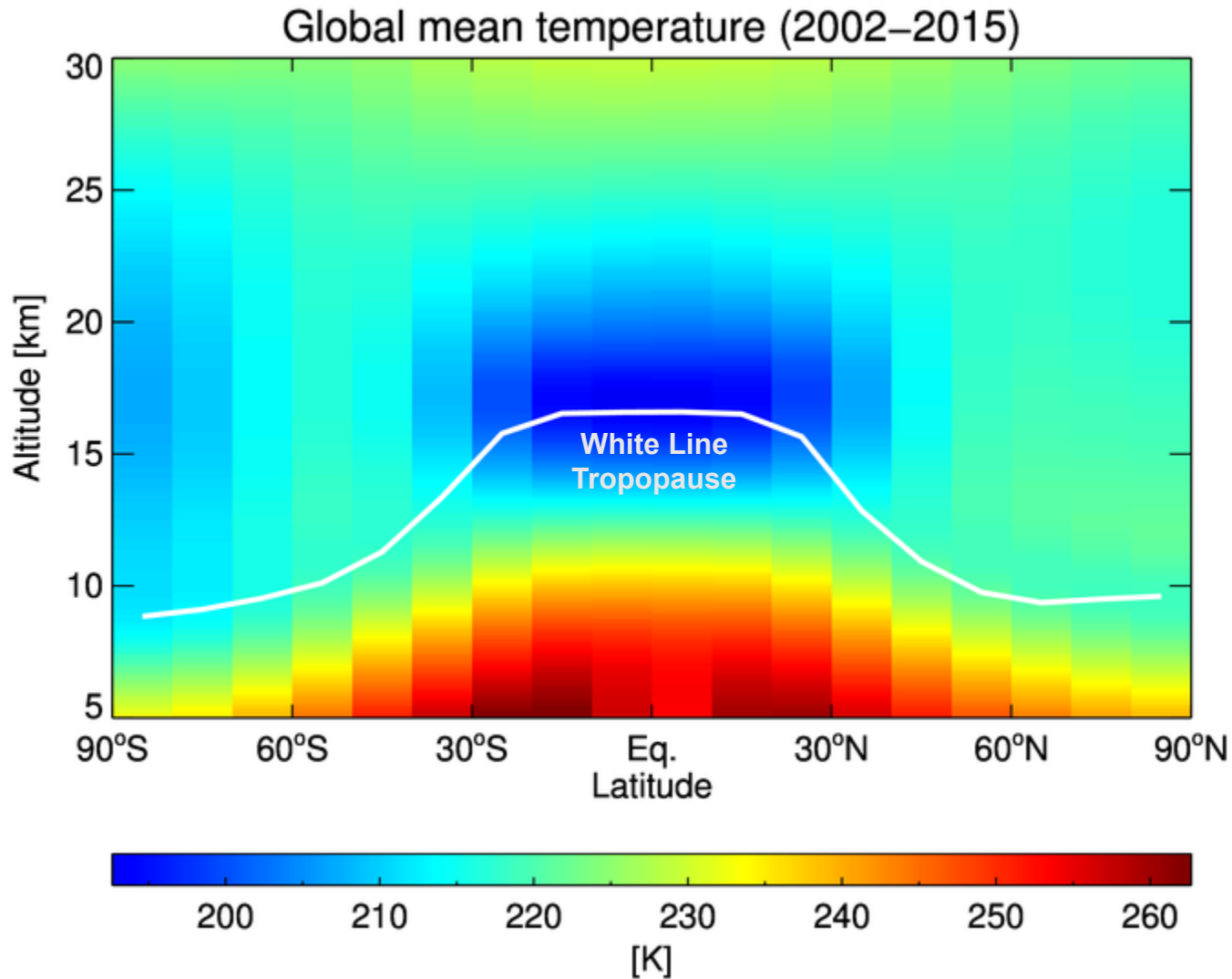
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Dry adiabatic lapse rate

Temperature versus Altitude & Latitude



<http://www.tschmidt.eu/ro/ENG/klima.html>

Temperature versus Altitude, Ocean

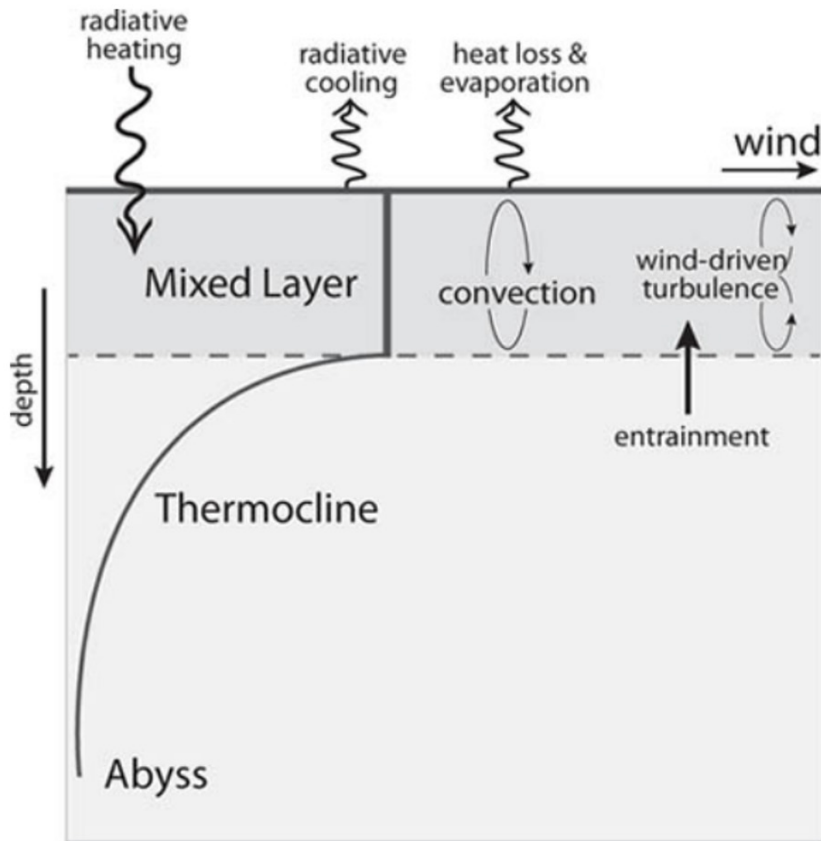


Figure 2.5. Schematic of the vertical structure of the ocean, emphasizing the mixed layer. In the mixed layer, typically 50–100 m deep, turbulence and convection act to keep the temperature relatively uniform in the vertical. Below this layer, temperature changes over a depth of a few hundred meters, in the *thermocline*, before becoming almost uniform at depth, in the *abyss*. Adapted from Marshall and Plumb, 2007.

Climate And The Oceans, Vallis

Temperature versus Altitude, Ocean

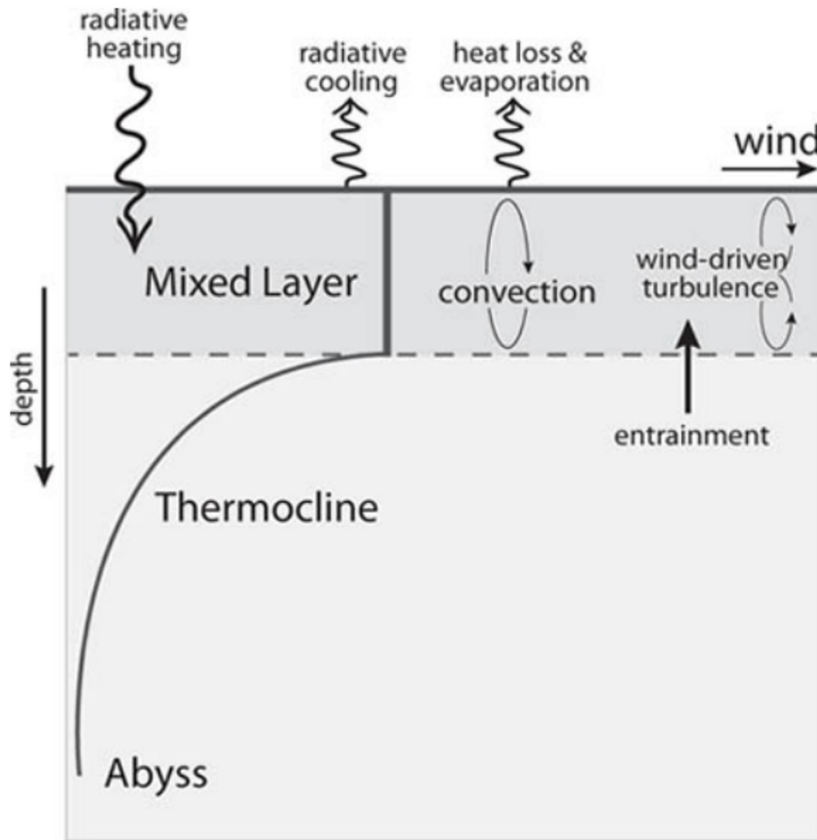


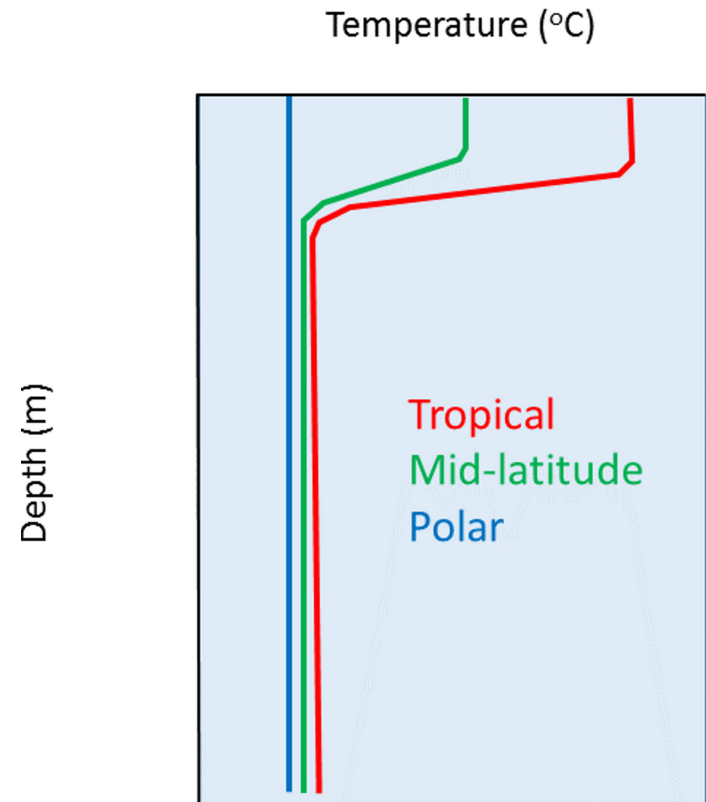
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THE ENHANCED GREENHOUSE EFFECT

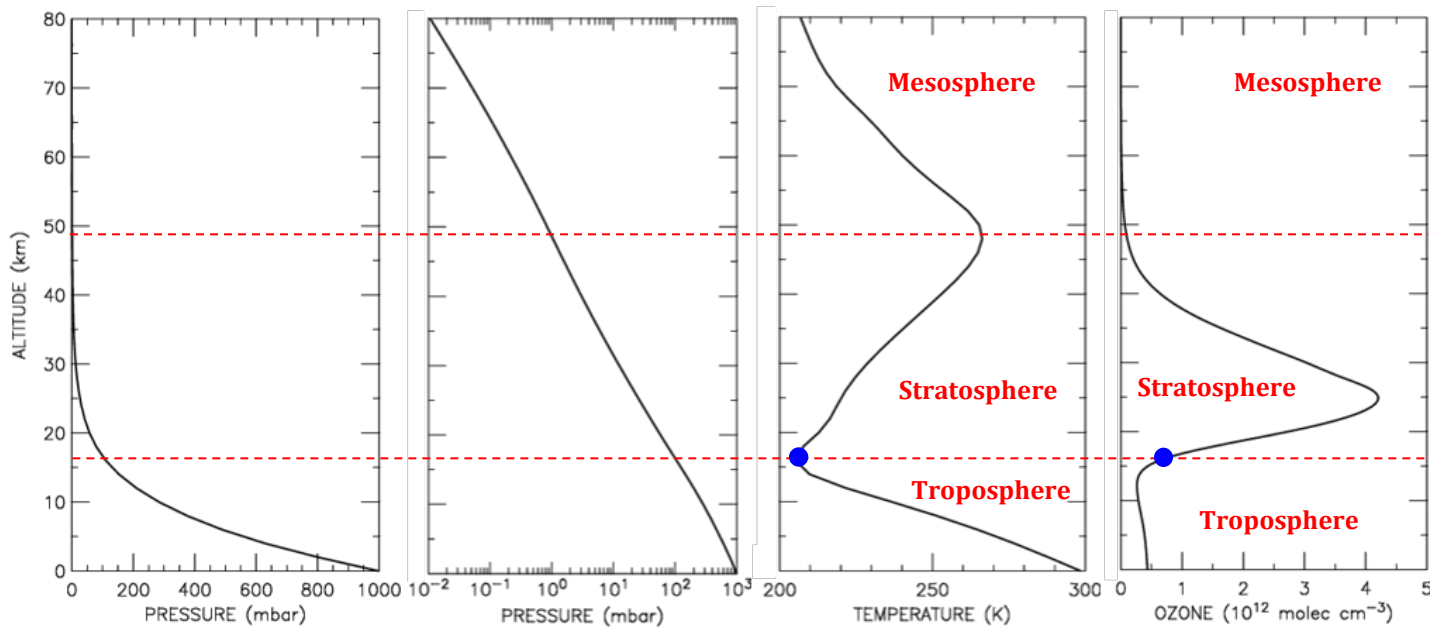
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The amount of water vapour in our atmosphere depends mostly on the temperature of the surface of the oceans; most of it originates through evaporation from the ocean surface and is not influenced directly by human activity. Carbon dioxide is different. Its amount has changed substantially – by nearly 40% so far – since the Industrial Revolution, due to human industry and also because of the removal of forests (see Chapter 3).



<https://rwu.pressbooks.pub/webboceanography/chapter/6-2-temperature>

Temperature versus Altitude

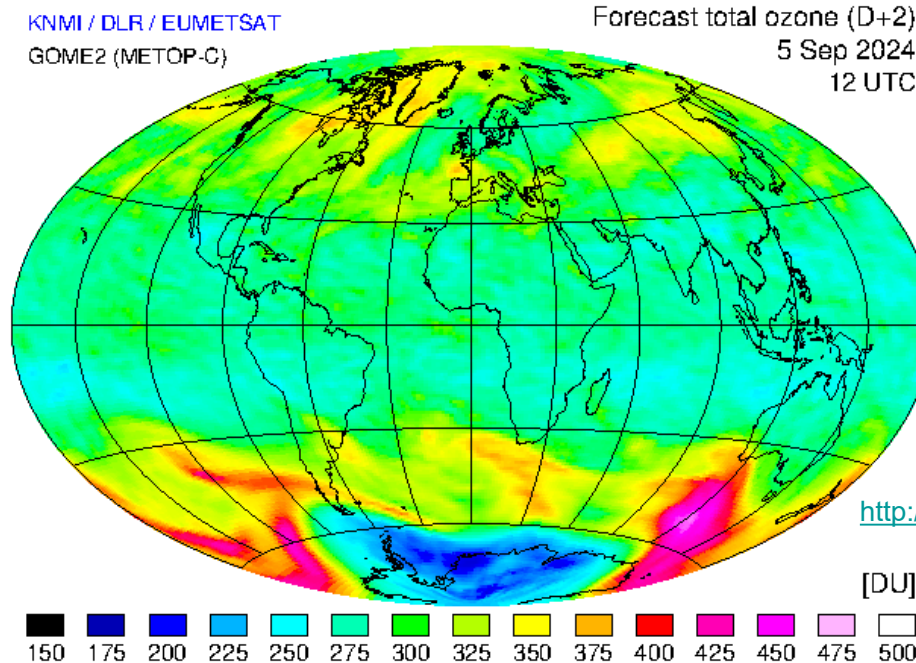


- T falls wrt increasing altit until the tropopause, then rises wrt altit until the stratopause, then falls wrt to rising altitude

Fourth chart expresses abundance of ozone concentration, or ozone density, or $[\text{O}_3]$, in units of molecules / cm^3

The Ozone Layer

According to *Chemistry in Context*, if all of the ozone in Earth's atmosphere could be isolated and brought to the surface at a pressure of 1 atmosphere and a temperature of 15°C), the resulting gas would have a thickness of **0.25 inch**



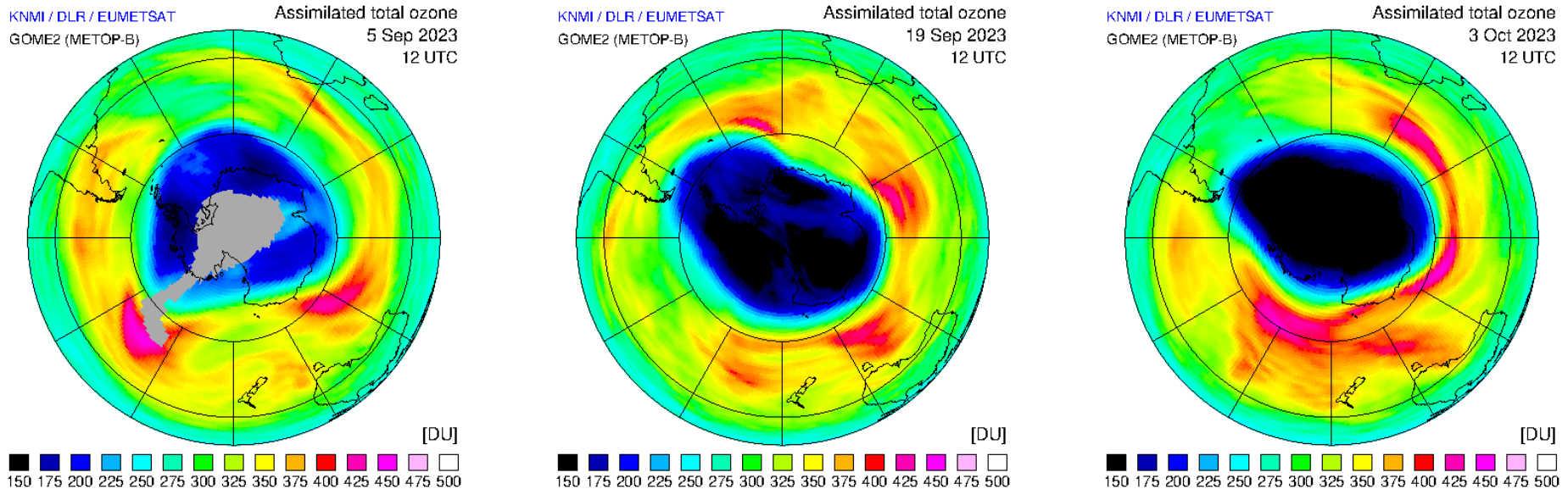
Mathematically:

$$\text{Ozone Column} = \int_{\text{Ground}}^{\text{Top of Atmosphere}} [\text{O}_3(z)] dz$$

Units : $[\text{O}_3(z)]$ in $\text{molecule}/\text{cm}^3$ and z in cm, leading to Ozone Column in $\text{molecule}/\text{cm}^2$

$$\text{Mathematically, } 1 \text{ DU} = 2.687 \times 10^{16} \text{ molecule}/\text{cm}^2$$

Seasonal Evolution of Ozone Hole



<http://www.temis.nl/protocols/O3global.html>

1 Dobson Unit is defined to be a 0.01 millimeter thickness of air, at “standard temperature and pressure”
Today we have about 300 Dobson Units (CC) = 300 x 0.01 millimeter = 3 millimeter or 0.3 cm = 0.12 inch
of ozone, isolated and compressed to STP, between us and outer space.

Global Average Ozone: 300 DU=3 mm



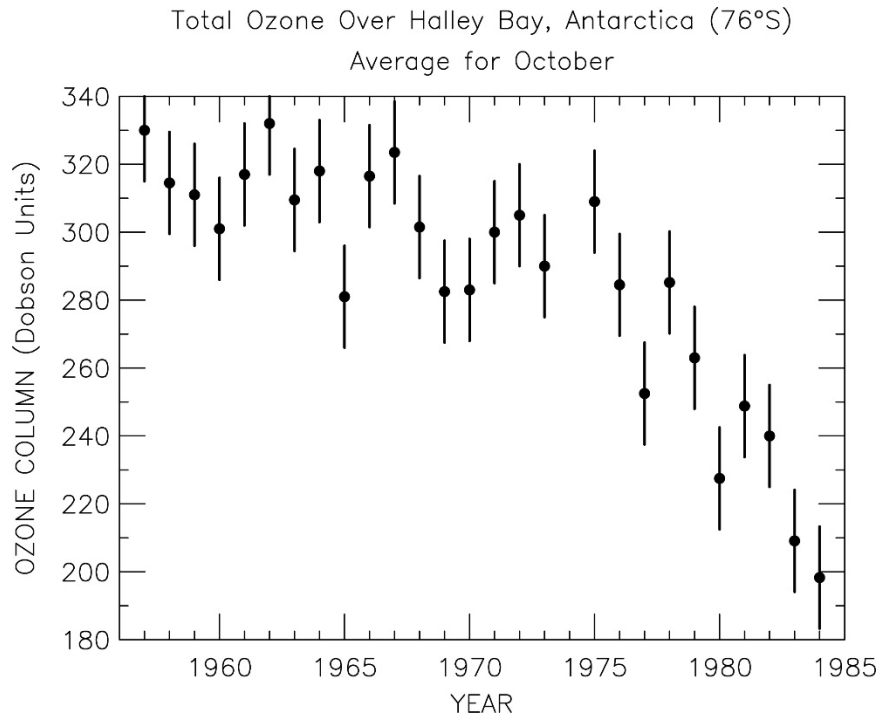
Ozone Hole Average: 100 DU=1 mm



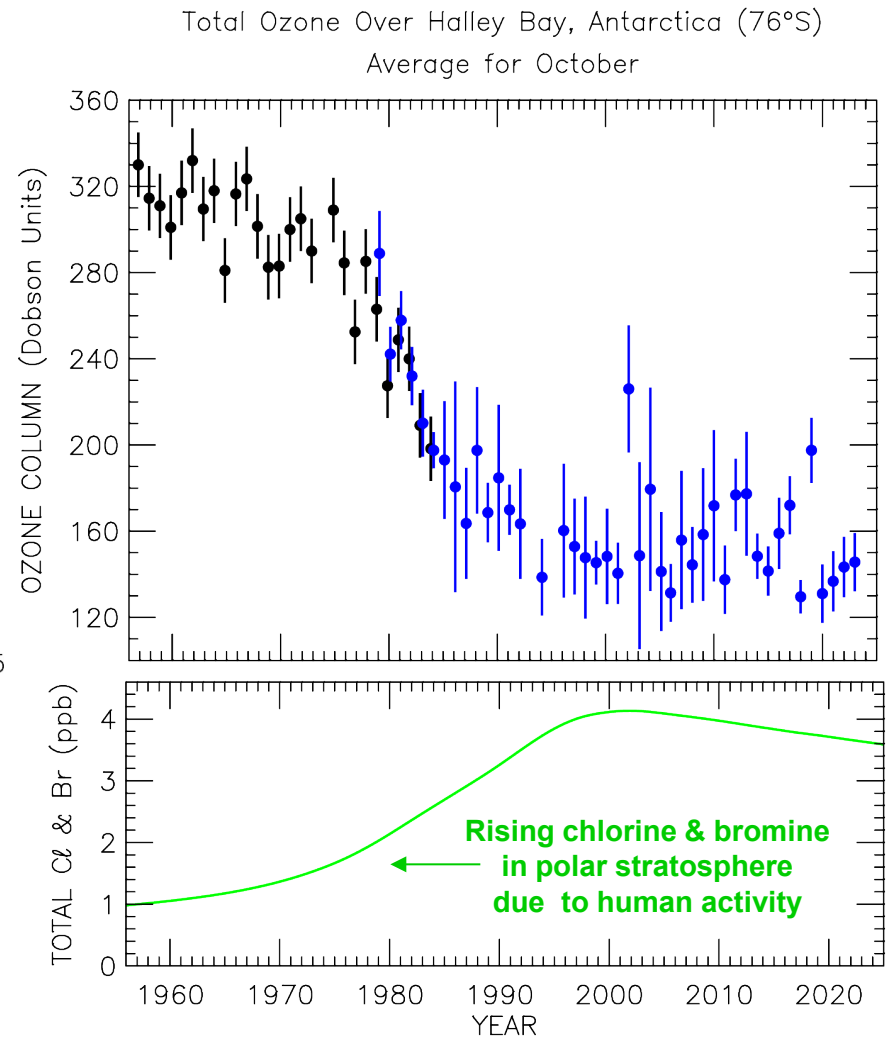
Earth's Atmosphere – Effect of Humans

Stratospheric Ozone – shields surface from solar UV radiation

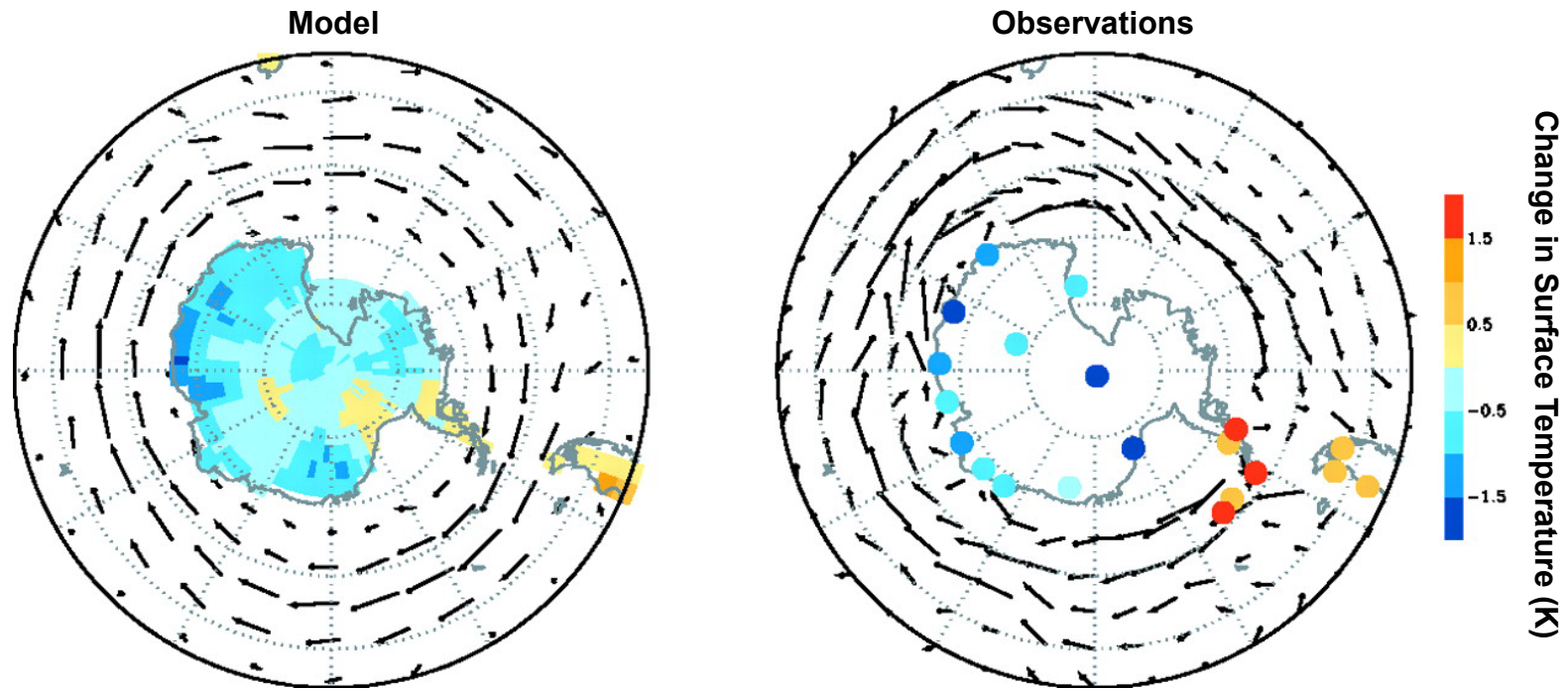
Update



After Farman *et al.*, Large losses of total ozone in Antarctica reveal Seasonal ClO_x/NO_x interaction, *Nature*, 315, 207, 1985.



The Ozone Hole may have shielded the Antarctic surface from warming!



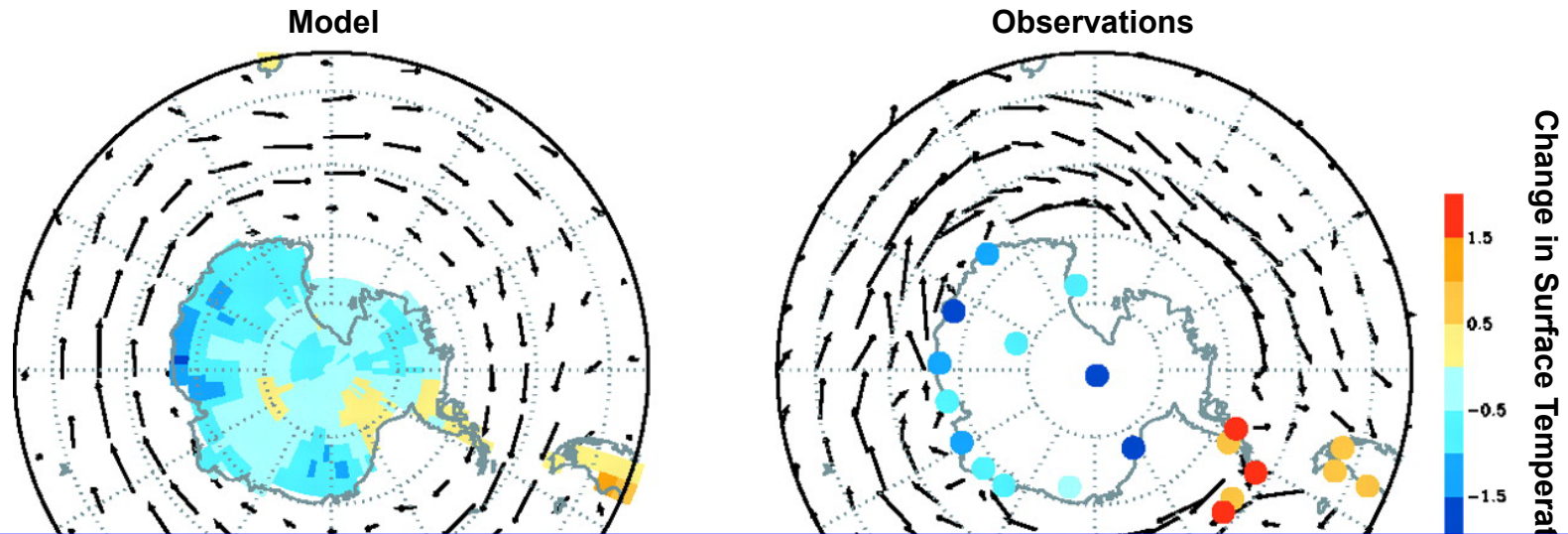
Simulated and observed changes in surface temperature (K) and wind speed, 1969 to 2000, averaged over December to May. The longest wind vector corresponds to 4 m/s.

Gillett and Thompson, *Science*, 2003

As ozone depletion occurs:

The positive phase of the southern annular mode (SAM) increases, causing Antarctic surface westerlies to intensify, resulting in cooling of Antarctic continent

The Ozone Hole may have shielded the Antarctic surface from warming!



SAM: difference in zonal mean sea-level pressure between 40°S and 65°S. The pattern associated with SAM is a nearly annular pattern with a large low pressure anomaly centered on the South Pole and a ring of high pressure anomalies at mid-latitudes. The SAM effects storm tracks, precipitation patterns, etc.

http://www.climate.be/textbook/chapter5_node6.html

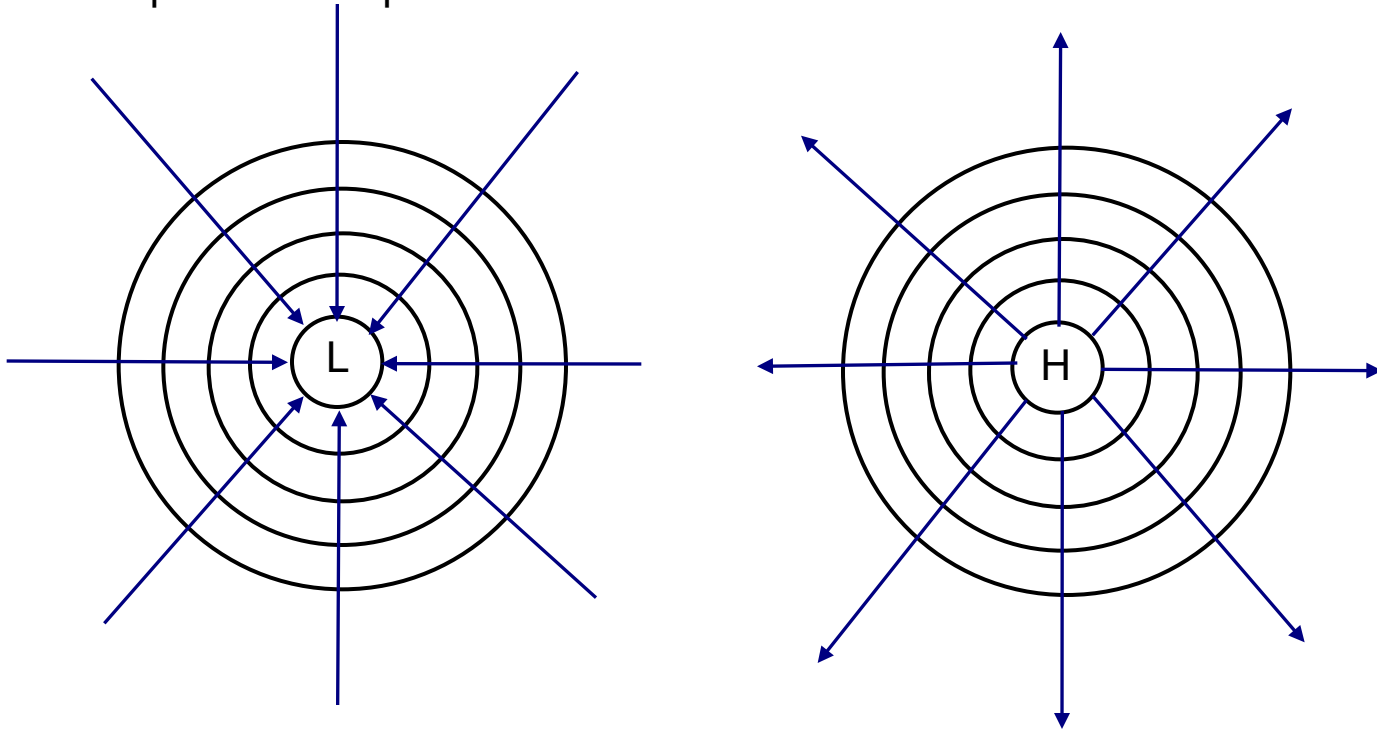
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Coriolis Force

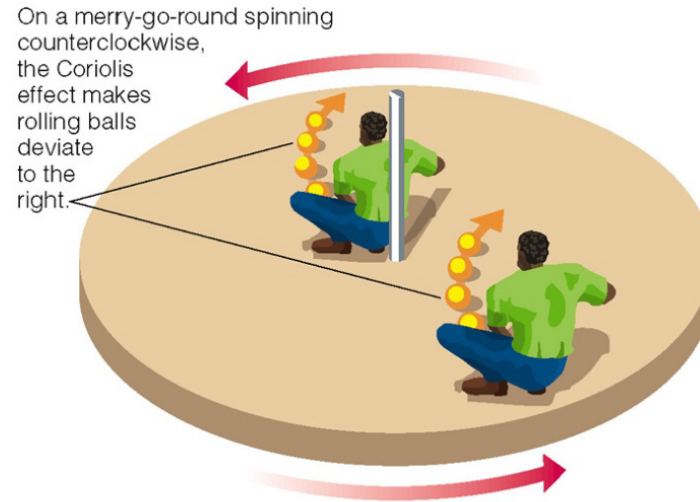
So far, we've reviewed temperature, pressure, and the balance between solar energy input to the atmosphere and terrestrial radiation leaving the atmosphere.

There's one more piece of the puzzle that we need to be familiar with.



In general, air moves from areas of high pressure to areas of low pressure.
In the absence of external forces, air will move in a straight line, following pressure gradients

Coriolis Force



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<http://lasp.colorado.edu/~bagenal/3720/CLASS15/15EVM-Dyn1.html>

Earth's rotation provides an apparent force that deflects air
to the right in the Northern Hemisphere,
to the left in the Southern Hemisphere.

Force is proportional to $\sin(\text{latitude})$, so vanishes at the equator

Geostrophy

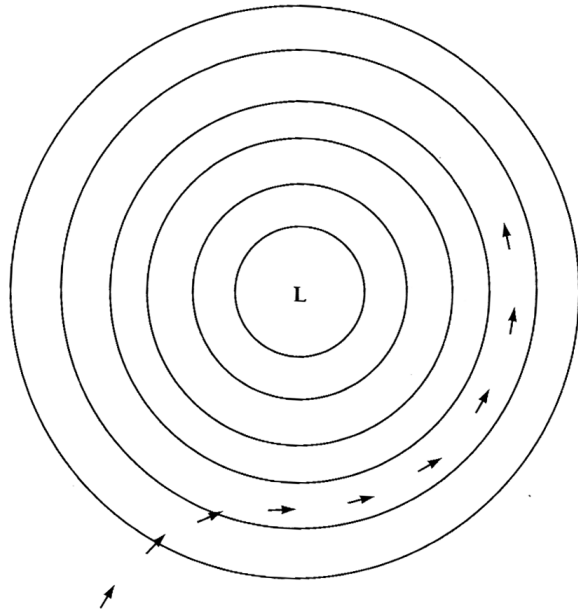


Figure 8.16 Track of an air parcel in the vicinity of a low pressure region in the Northern Hemisphere. The parcel is initially at rest but then adjusts to the pressure gradient force and the Coriolis force to achieve geostrophic balance.

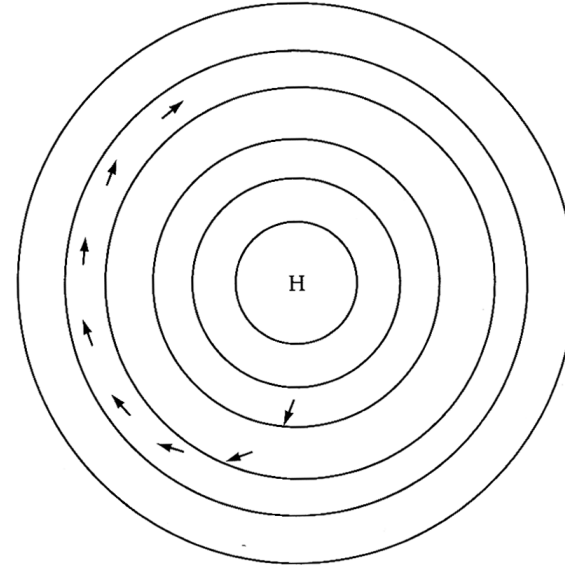


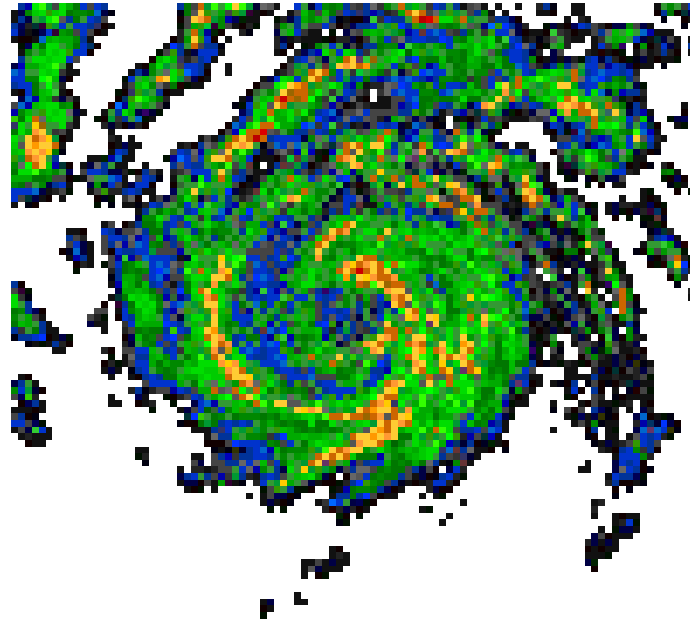
Figure 8.17 Same situation as in 8.16, except that the parcel is in the vicinity of a high pressure region in the Northern Hemisphere.

From "The Atmospheric Environment", M. B. McElroy

Geostrophic balance: balance between Coriolis Force and pressure gradient

Geostrophy

NH Weather System:



Cyclonic Flow: when the wind swirls
counter-clockwise in the NH

Hurricane: Cyclonic flow occurring in the N Atlantic or NE Pacific Ocean east of the dateline.

Typhoon: Cyclonic flow occurring in the NW Pacific Ocean, west of the dateline.

Cyclones: Cyclonic flow occurring in the South Pacific and Indian Ocean.

Atmospheric Circulation

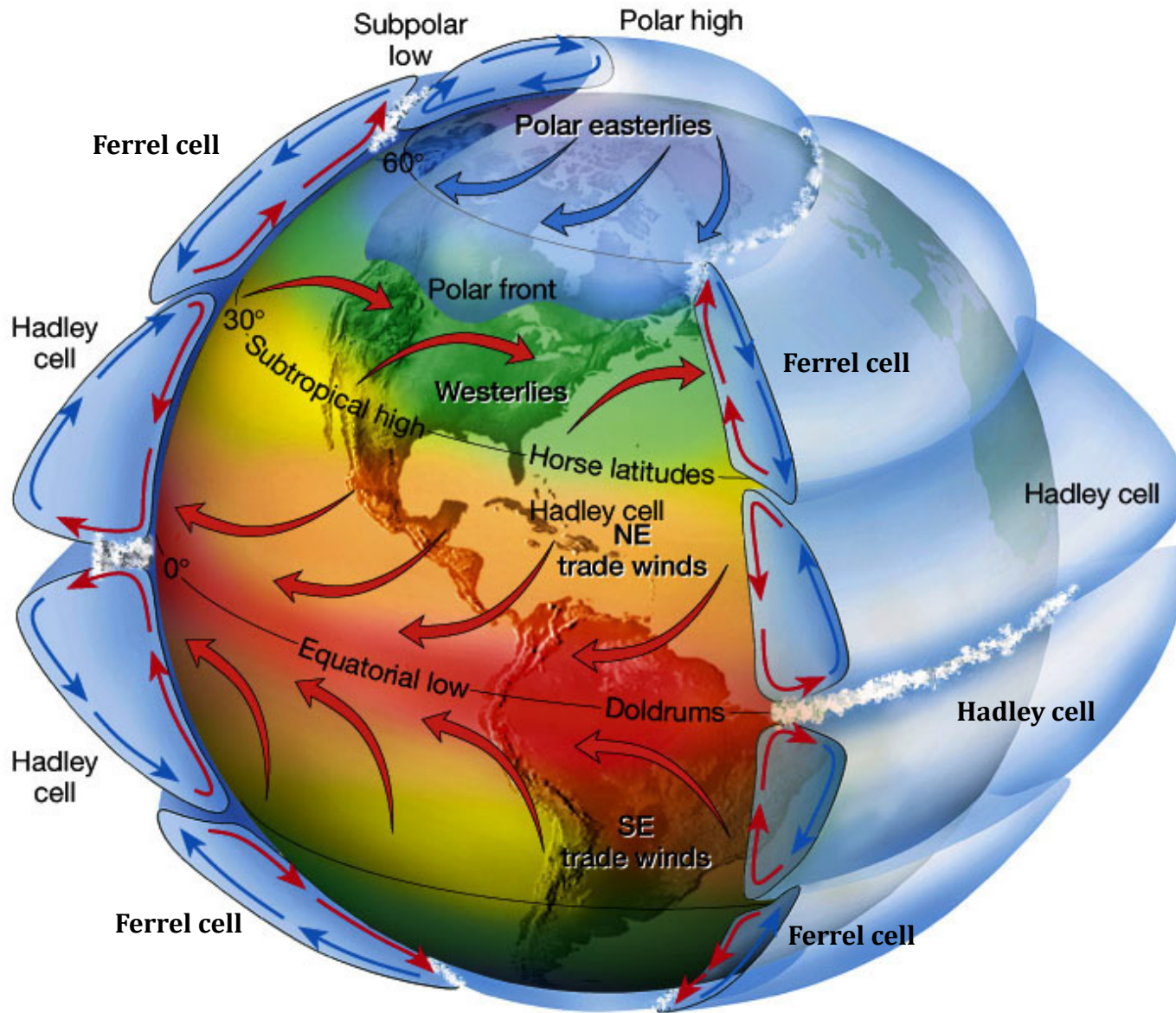


Figure 7.5 in *The Atmosphere*, 8th edition, Lutgens and Tarbuck, 8th edition, 2001; <http://www.ux1.eiu.edu/~cfjps/1400/circulation.html>

Oceanic Circulation

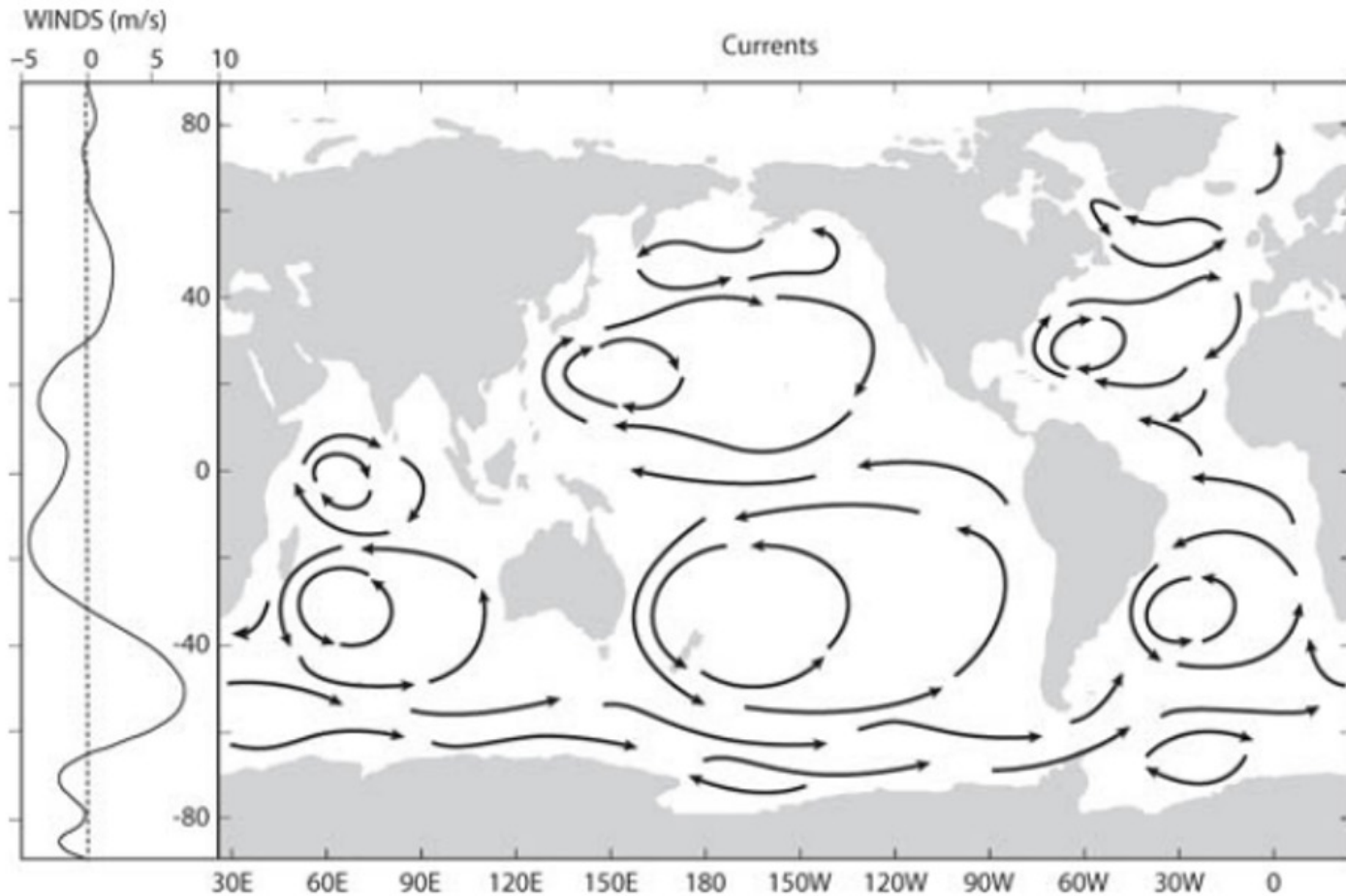
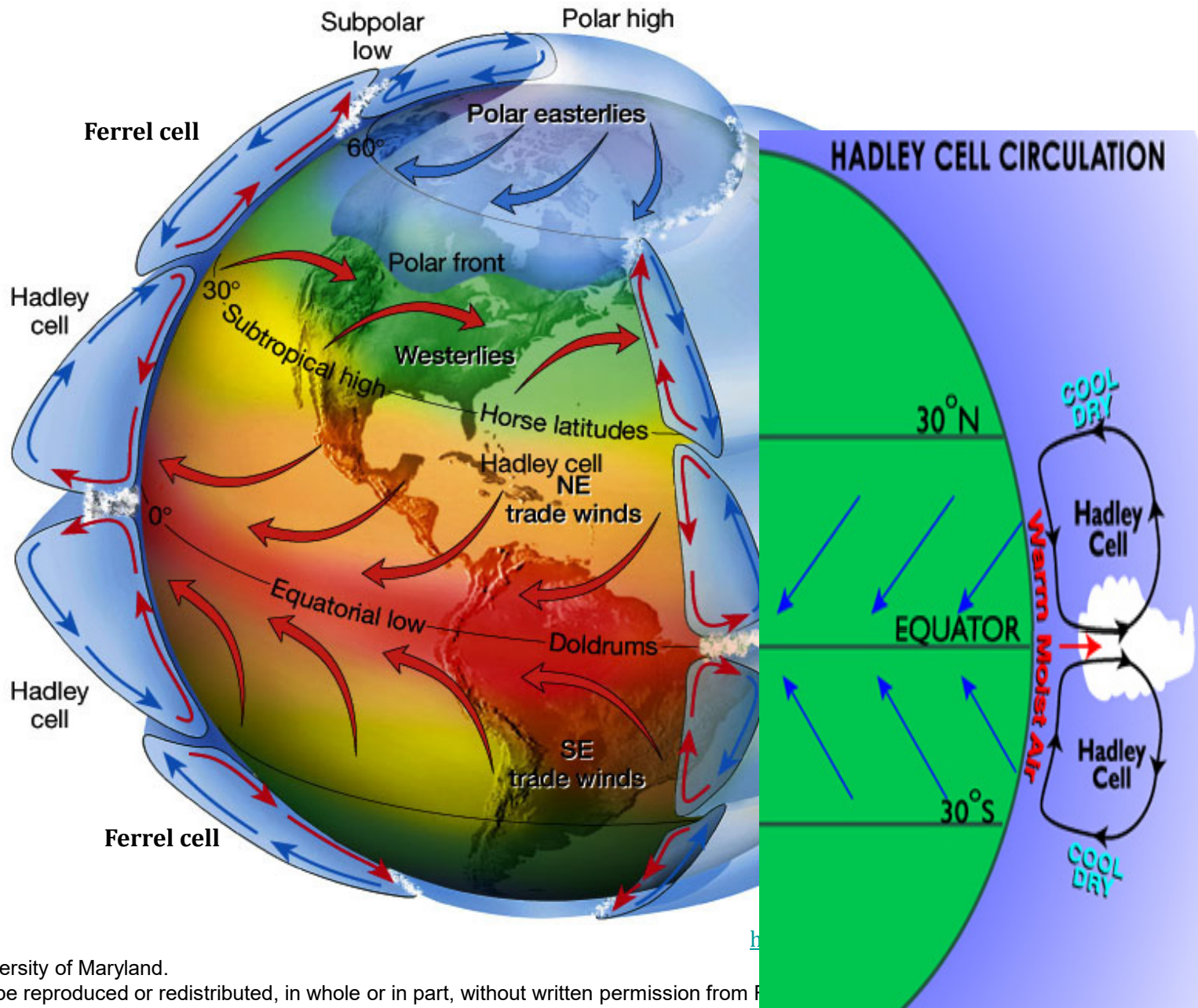


Figure 2.3. A schematic of the main surface currents of the world's oceans. The panel at the left shows the zonally averaged zonal (i.e., east-west) surface winds.

Climate And The Oceans, Vallis

Atmospheric Circulation



As CO₂ and other GHGs rise:
Hadley Cell becomes more energetic
WWDD: Wet gets wetter, dry gets drier
Deserts expand poleward

REVIEW ARTICLE

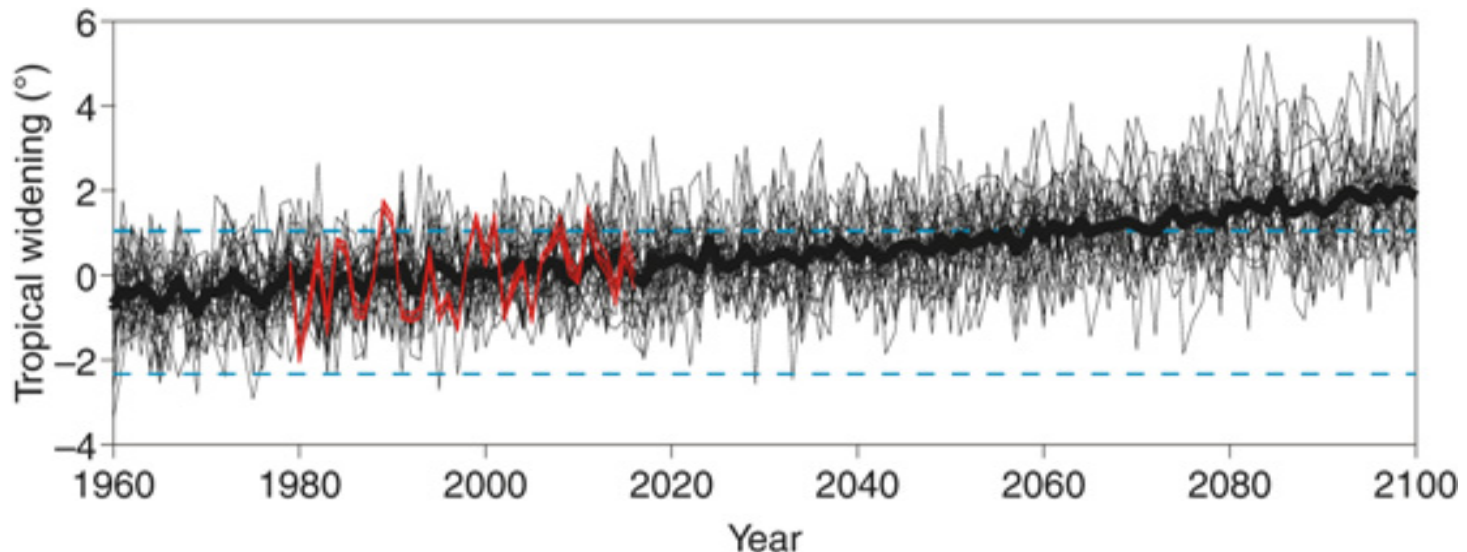
<https://doi.org/10.1038/s41558-018-0246-2>

nature
climate change

Re-examining tropical expansion

Paul W. Staten¹, Jian Lu^{2*}, Kevin M. Grise³, Sean M. Davis^{4,5} and Thomas Birner⁶

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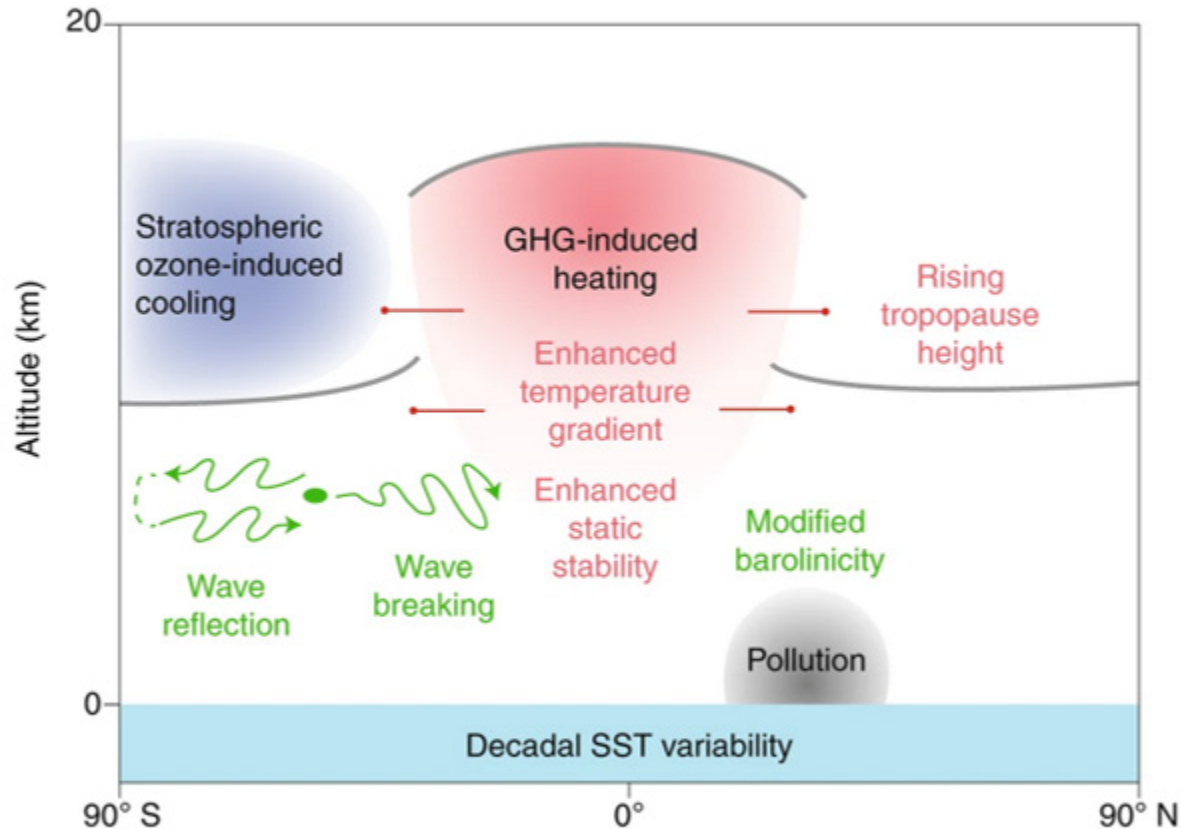
Change in the latitudinal width of the tropics relative to 1981–2010 mean from satellite observations (red) and climate models (thin black lines), along with the multi-model mean (thick black). The blue dashed lines show the 2σ range of the width of the tropics due to natural variability for pre-industrial levels of GHGs.

From Staten *et al.*, *Nature Climate Change*, 2018. <https://www.nature.com/articles/s41558-018-0246-2>

Tropical Expansion: Causal Factors

Fig. 3: Factors and mechanisms for tropical expansion.

From: [Re-examining tropical expansion](#)



The key factors hypothesized to be responsible for the recent tropical expansion are tropical upper-tropospheric warming related to GHG forcing, enhanced extratropical stratospheric cooling related to O₃ depletion in the Southern Hemisphere, emissions of black carbon and tropospheric ozone (pollution, primarily over the Northern Hemisphere) and decadal SST variability and trends. A green dot is used to denote the source of Rossby waves.

Staten *et al.*, *Nature Climate Change*, 2018. <https://www.nature.com/articles/s41558-018-0246-2>

Tropical Expansion: One Important Consequence

Article | [Open access](#) | Published: 11 September 2023

New insights into the poleward migration of tropical cyclones and its association with Hadley circulation

[U. Anjana](#)  & [Karanam Kishore Kumar](#)

[Scientific Reports](#) **13**, Article number: 15009 (2023) | [Cite this article](#)

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Abstract

Recent investigations have shown a robust signature of poleward migration of the tropical cyclone latitudes using observations and climate model simulations. Most of these studies invoked the role of the Hadley circulation (HC) expansion in the poleward shifting of tropical cyclones. However, none of these studies focused on the dissection of the zonally asymmetric HC into ascending and descending regions at regional scales, which holds the key in establishing the association between these two phenomena. Here, we are reporting the poleward migration of tropical cyclones and their association with ascending region boundaries of the HC at regional scales for the first time. The results emphatically show that the tropical cyclone latitudes as well as latitudes of maximum lifetime intensity vary in tandem with boundaries of the ascending region of the HC as compared to its descending region thus providing a vital clue on processes governing poleward migration of tropical cyclones.

Anjana and Kumar, *Nature Climate Change*, 2023. <https://www.nature.com/articles/s41598-023-42323-7>

Next Lecture: Climates of the Past

Next Reading:

Chemistry in Context, Secs 2.2, 3.0, 3.1, 3.2 (~14 pgs)

as well as 8 pages from *Global Warming: The Complete Briefing* by Houghton
7 pages from *Paris Beacon of Hope*

Derivation of the Barometric Law

Extra Slide #1

Assume a sample volume is at rest with respect to vertical motion :

$$p(z) - p(z + \Delta z) = \rho \text{ grav } \Delta z$$

in other words, the pressure difference between z and $z + \Delta z$

is equal to the weight of air contained in a volume of unit horiz area.

Using calculus:

$$\frac{dp}{dz} = -\rho(z) \text{ grav}$$

Writing the gas law as $p = R_{\text{EARTH}} \rho T$

$$\text{where } R_{\text{EARTH}} = 8.3143 \times 10^7 \frac{\text{ergs}}{\text{K mole}} \times \frac{\text{mole}}{28.8 \text{ gm}} = 2.87 \times 10^6 \text{ ergs/ K gm}$$

and substiting gives:

$$\frac{dp}{dz} = - \frac{p \text{ grav}}{R_{\text{EARTH}} T}$$

Or

$$\frac{dp}{p} = - \frac{dz}{H} \quad \text{where } H = \frac{R_{\text{EARTH}} T}{\text{grav}}$$

The solution of this ODE is:

$$p(z) = p(z=0)e^{-z/H}$$