AGU PUBLICATIONS Geophysical Research Letters Supporting Information for Climatology of cloud-top radiative cooling in marine shallow clouds Youtong Zheng^{1,4}, Yannian Zhu², Daniel Rosenfeld^{2,3}, and Zhanqing Li¹ Affiliations: ¹Earth System Science Interdisciplinary Center, University of Maryland, College Park, Maryland, 20742, USA. ²Nanjing University, Nanjing, China ³Herew University of Jerusalem, Jerusalem, Israel ⁴Now at GFDL/AOS program, Princeton University, Princeton, New Jersey Contents of this file 1. Text S1~S2 2. Figures S1~S5 3. Table S1

Text S1: Radiative transfer model

The radiative transfer model we use is the Santa Barbara DISORT Atmospheric Radiative Transfer model (Ricchiazzi et al., 1998). We specify the vertical grids with resolutions of 50 m from the surface to 2.25 km and the grid spacing increases with the altitude until the top of the atmosphere, leading to a total of ~ 60 grids in the vertical. The ozone profile and greenhouse gas concentrations are set to default values. The cloud optical depth is uniformly distributed throughout the cloud layer. The wavelength ranges of longwave and shortwave are set as $5 \sim 40$ μ m and 0.1 ~ 5 μ m, respectively. The wavelength increment is 0.1 μ m for shortwave and 0.2 μ m for longwave.

Text S2: Configuration of the neural network model

Our NN has a total of four layers. The input and output layers have 25 and 5 nodes respectively, which matches the number of input and output variables. Between them are two fully connected hidden layers with 256 nodes. This adds up to a total of 73733 learnable parameters. We use the Rectified Linear Unit (ReLU) for activation function and the Adam optimizer with a mean squared error loss function. Given the large number of training samples, the specific choices of the hyper-parameters make little difference to the performance. The input data are normalized and shuffled before the training. The total training time was about 7 minutes on a single graphics processing unit.







Figure S2: Probability density functions of the ratio between the temperature at 500 hPa (as an approximation for T_a in Eq. 2) and cloud-top temperature.













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	Input variables	Unit	Output variables	Unit
	Cloud optical depth	Unitless	Cloud top radiative cooling, ΔF	W m ⁻²
	Cloud droplet effective radius	μm	Cloud top longwave cooling, ΔF_{LW}	W m ⁻²
	Cloud top temperature	Κ	Cloud top shortwave heating, ΔF_{SW}	W m ⁻²
	Solar zenith angle	degree	Cloud base longwave heating	W m ⁻²
	Sea surface temperature	Κ	Cloud longwave radiative effect	W m ⁻²
	Absolute temperature from 1000	Κ		
	hPa to 100 hPa with 100 hPa			
	interval			
	Relative humidity from 1000 hPa	%		
	to 100 hPa with 100 hPa interval			
125	Table 1: Input and output va	riables for th	e Neural Network. The CTRC variables	s used in
126	this	study are hig	ghlighted in bold.	
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Reference

Ricchiazzi, P., Yang, S., Gautier, C., & Sowle, D. (1998). SBDART: A research and teaching software tool
for plane-parallel radiative transfer in the Earth's atmosphere. *Bulletin of the American Meteorological Society, 79*(10), 2101-2114.